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PAPER

# Formation of ultracold Rb<sub>2</sub> molecules in the $v'' = 0$ level of the $a^3\Sigma_u^+$ state *via* blue-detuned photoassociation to the $1^3\Pi_g$ state†

M. A. Bellos,<sup>\*a</sup> D. Rahmlow,<sup>a</sup> R. Carollo,<sup>a</sup> J. Banerjee,<sup>a</sup> O. Dulieu,<sup>b</sup> A. Gerdes,<sup>c</sup>  
E. E. Eyler,<sup>a</sup> P. L. Gould<sup>a</sup> and W. C. Stwalley<sup>a</sup>

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We report on the observation of blue-detuned photoassociation in Rb<sub>2</sub>, in which vibrational levels are energetically above the corresponding excited atomic asymptote. <sup>85</sup>Rb atoms in a MOT were photoassociated at short internuclear distance to levels of the  $1^3\Pi_g$  state at a rate of approximately  $5 \times 10^4$  molecules s<sup>-1</sup>. We have observed most of the predicted vibrational levels for all four spin-orbit components;  $0_g^+$ ,  $0_g^-$ ,  $1_g$ , and  $2_g$ , including levels of the  $0_g^+$  outer well. These molecules decay to the metastable  $a^3\Sigma_u^+$  state, some preferentially to the  $v'' = 0$  level, as we have observed for photoassociation to the  $v' = 8$  level of the  $1_g$  component.

## 1 Introduction

Photoassociation (PA) of ultracold atoms is a powerful spectroscopic technique to produce and study ultracold molecules.<sup>1,2</sup> Most photoassociation experiments access vibrational levels that are red-detuned from atomic transitions. Blue-detuned PA, where vibrational levels are energetically above their corresponding atomic asymptote, was first proposed to probe quasibound states<sup>3</sup> and form ultracold Rb<sub>2</sub><sup>4</sup> and KRb molecules.<sup>5</sup> Blue-detuned photoassociation was first observed<sup>6</sup> in our laboratory; however, molecular assignments have remained elusive due to relatively small signals. Blue-detuned photoassociation has also been observed using an intense femtosecond laser,<sup>7</sup> which simultaneously drove resonant and non-resonant transitions to a variety of states, making molecular assignments difficult to perform.

There are two cases where blue-detuned photoassociation could occur: (1) in a local minimum of a potential energy curve repulsive at long range (as in the case here with the  $1^3\Pi_g$  state of Rb<sub>2</sub>) or (2) in a well that contains a potential barrier and vibrational levels above the atomic asymptote (for instance the  $2^1\Sigma_g^+$  state in Rb<sub>2</sub>).<sup>8</sup> Although there is no fundamental difference between blue-detuned and red-detuned photoassociation, blue-detuned photoassociation generally occurs at small internuclear distances where the Franck–Condon factors for photoassociation are smaller. Furthermore blue-detuned photoassociation rates may be reduced by optical shielding effects<sup>9</sup> where colliding

atoms are prevented from reaching small internuclear distances. However an estimate based on ref. 10 indicates that these effects should be negligibly small for our experimental configuration.

Here, we demonstrate blue-detuned photoassociation to the short-range  $1^3\Pi_g$  state of <sup>85</sup>Rb<sub>2</sub> as shown in Fig. 1. This is the first time a free-bound transition to the quasibound  $1^3\Pi_g$  state has been directly observed. The  $1^3\Pi_g$  state has been previously observed through transitions in heat pipe ovens<sup>4,5,11</sup> and on liquid helium droplets.<sup>12</sup> Photoassociation at short internuclear distance for red-detunings has also been demonstrated<sup>13,14</sup> on the B<sup>1</sup>Π state of LiCs, yielding ground rovibrational X<sup>1</sup>Σ<sup>+</sup> state molecules.<sup>15</sup> In both these cases, the relatively high efficiency of the photoassociation process at short range is somewhat surprising.

The production of ultracold Rb<sub>2</sub> in the  $v'' = 0$ ,  $J'' = 0$  level of the  $a^3\Sigma_u^+$  state has previously been achieved<sup>18</sup> through the technique of magnetoassociation followed by STIRAP transfer. The present paper demonstrates a complementary way to reach the same level. The main advantage of the pathway that we demonstrate is experimental simplicity, as it proceeds through a simple PA step followed by spontaneous emission. A distribution of vibrational levels is created in the  $a^3\Sigma_u^+$  state, with, in some cases, a significant proportion in the lowest one. A notable difference between the two techniques is that magnetoassociation typically requires temperatures on the order of 100 nK (close to quantum degeneracy), while photoassociation can occur at higher temperatures, such as in magneto-optical traps with temperatures on the order of 100 μK. Also, photoassociation followed by spontaneous emission is irreversible and can provide continuous accumulation of molecules.

## 2 The $1^3\Pi_g$ potential energy curves

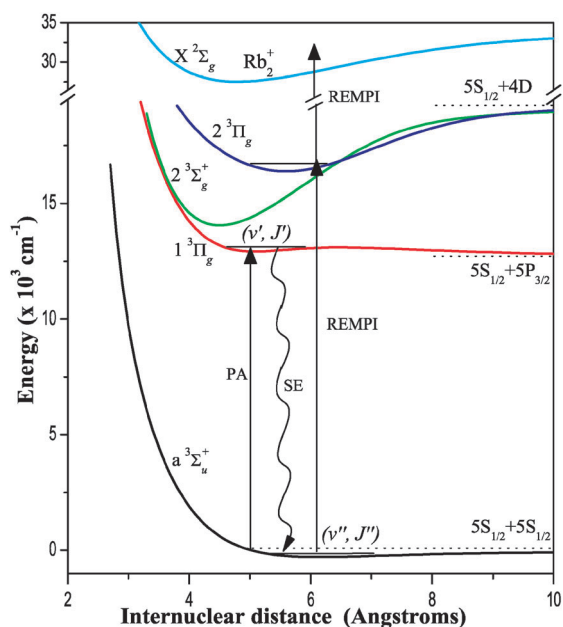
The spin-orbit coupling of the  $1^3\Pi_g$  state with neighboring molecular states that correlate to the same asymptotic limit

<sup>a</sup> Department of Physics, University of Connecticut, Storrs, Connecticut 06269-3046, USA. E-mail: bellos@phys.uconn.edu

<sup>b</sup> Laboratoire Aimé Cotton, CNRS, Université Paris-Sud, bât. 505, 91405 Orsay, France

<sup>c</sup> Computing and Storage Services, Regional Computer Centre for Lower Saxony, Leibniz Universität, Hannover, Germany

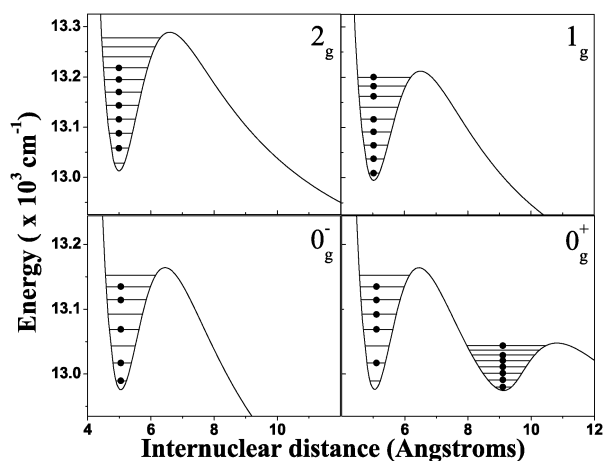
† Electronic supplementary information (ESI) available:  $0_g^+$ ,  $0_g^-$ ,  $1_g$ , and  $2_g$  potential energy curves. See DOI: 10.1039/c1cp21383k



**Fig. 1** Scheme for producing and detecting ultracold metastable  $\text{Rb}_2$  molecules. Blue-detuned photoassociation (PA) from free atoms to bound levels  $(v', J')$  of the  $1^3\Pi_g$  state is followed by spontaneous emission (SE) to a variety of  $(v'', J'')$  levels of the  $a^3\Sigma_u^+$  state. Molecule detection through resonantly enhanced multiphoton ionization (REMPI) is a two step process achieved by first exciting molecules to an intermediate state ( $2^3\Sigma_g^+$  or  $2^3\Pi_g$ ), immediately followed by photoionization to produce  $\text{Rb}_2^+$ . The horizontal dotted lines indicate the positions of atomic asymptotes. The potential energy curves for  $\text{Rb}_2$  and  $\text{Rb}_2^+$  are from ref. 16 and 17, respectively.

results in four distinct components,  $1^3\Pi_g(\Omega = 0^+)$ ,  $1^3\Pi_g(\Omega = 0^-)$ ,  $1^3\Pi_g(1)$ , and  $1^3\Pi_g(2)$ . Where the integer in parenthesis,  $\Omega$ , is the projection of the total electronic angular momentum on the internuclear axis,  $g$  is the parity of the electronic wavefunction by reflection through the center of mass, and  $(\pm)$  is the symmetry of the electronic wavefunction by reflection through a plane containing the internuclear axis. These states can be expressed more compactly as  $0_g^+$ ,  $0_g^-$ ,  $1_g$ , and  $2_g$  using Hund's case (c) notation. Their potential energy curves and bound levels are plotted in Fig. 2.

These potential curves are calculated using a rotation-based diabaticization method within a quasidegenerate perturbation theory.<sup>19</sup> The sixteen lowest adiabatic states of each relevant symmetry  $^3\Pi_g$ ,  $^1\Pi_g$ ,  $^3\Sigma_g^+$ ,  $^1\Sigma_g^+$  in Hund's case (a) are obtained by the method described in ref. 20. This method is based on a representation of the  $\text{Rb}^+$  ionic cores by an effective core potential including scalar relativistic terms and core polarization. The electronic Hamiltonian of the related effective two-electron system is expressed in a large basis set of Gaussian orbitals. A full configuration interaction leads to adiabatic potential curves for each relevant molecular symmetry labeled in Hund's case (a). Following ref. 19, the corresponding eigenstates are used as reference states at the internuclear distance of 40 a.u. (1 a.u. = 0.527177 Å), which are considered as representative of the separated-atom states with a reasonable accuracy. At this distance the potential energies including spin-orbit interaction are obtained after diagonalizing the Hamiltonian  $H_{\text{so}}^{\text{adia}} = H^{\text{adia}} + H_{\text{so}}$ , where the diagonal  $H^{\text{adia}}$  matrix contains the adiabatic energies for all four symmetries



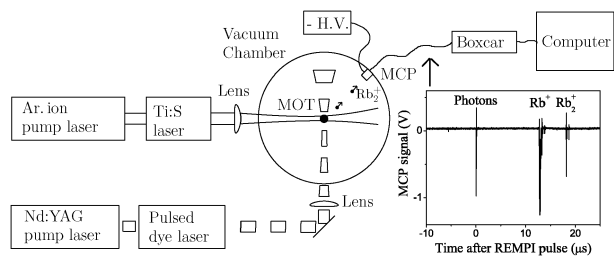
**Fig. 2**  $1^3\Pi_g$  potential energy curves with spin-orbit coupling, along with vibrational levels calculated by the LEVEL 8.0 program.<sup>21</sup> Dots ( $\bullet$ ) denote the experimentally observed vibrational levels. The levels that were unobserved most likely have a weaker photoassociation rate, due to low Franck-Condon factor overlaps. The  $0_g^+$  and  $0_g^-$  states are double well systems, with an inner and outer well. The outer well of the  $0_g^-$  state<sup>22,23</sup> (not shown) occurs at large internuclear distance and is red-detuned from the atomic asymptote.

above, and the coupling matrix  $H_{\text{so}}$  the relevant atomic spin-orbit coupling terms for the dissociation limits up to  $5^2S + 6^2P$ .

At each internuclear distance  $R$  between 5 a.u. and 40 a.u., a rotation  $\mathcal{R}$  of the subspace generated by the sixteen lowest adiabatic states is defined in order to maximize their overlap with the reference states above. This defines an effective Hamiltonian  $H^{\text{eff}}$  in an atomic-like basis, in which we introduce the  $H_{\text{so}}$  matrix elements to set up a Hamiltonian matrix  $H_{\text{so}}^{\text{eff}}$ . The diagonalization of  $H_{\text{so}}^{\text{eff}}$  at each  $R$  yields potential curves including  $R$ -dependent spin-orbit couplings, such as those shown in Fig. 2. Moreover, the inverse rotation  $\mathcal{R}^{-1}$  of  $H_{\text{so}}^{\text{eff}}$  back to the initial adiabatic states results in a non-diagonal matrix  $H_{\text{so}}^{\text{diab}}$ , where diagonal elements are the initial adiabatic potential curves, and off-diagonal terms are the  $R$ -dependent spin-orbit couplings between these states. This  $R$ -dependence is induced by the variation of the admixture of electronic states with internuclear distance. As noted in ref. 19, the efficiency of the model is mainly limited by the overlap of the adiabatic states at  $R$  with the reference states, which decreases from unity (at  $R = 40$  a.u. in the present case) to about 70% at  $R = 10$  a.u. As demonstrated in Section 4, these results represent a good basis for the interpretation of the experimental measurements.

### 3 Experiment

The setup consists of an  $^{85}\text{Rb}$  magneto-optical trap (MOT) holding  $\sim 10^6$  atoms at a temperature of  $\sim 125$   $\mu\text{K}$  with a density of  $\sim 10^{11}$  atoms per  $\text{cm}^3$ . The MOT trapping laser is locked 14 MHz below the  $|5S_{1/2}, F = 3\rangle \rightarrow |5P_{3/2}, F' = 4\rangle$  transition at 780 nm. A repump laser locked on resonance with the  $|5S_{1/2}, F = 2\rangle \rightarrow |5P_{3/2}, F' = 3\rangle$  transition is used to pump atoms that spontaneously decay to the  $|5S_{1/2}, F = 2\rangle$  state back to the  $|5S_{1/2}, F = 3\rangle$  state. Since our optical repumping is not perfect, the energy splitting between the two hyperfine states  $|5S_{1/2}, F = 2\rangle$  and  $|5S_{1/2}, F = 3\rangle$  of 0.1012  $\text{cm}^{-1}$  is one



**Fig. 3** Schematic diagram of the photoassociation, REMPI and detection systems. The inset shows the time of flight of photons, atomic ions, and molecular ions reaching the MCP detector.

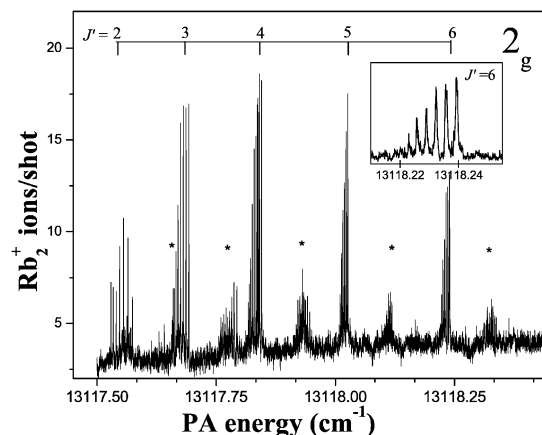
that routinely appears in our PA spectra in the form of weak “hyperfine ghost” lines. We were not able to fully eliminate these atomic “hyperfine ghost” lines from the spectra even after double checking for proper repump laser operation. A tunable cw Ti:sapphire laser (Coherent 899-29) with a power of  $\sim 700$  mW and a linewidth of 500 kHz is focused approximately to the size of the MOT ( $\sim 1$  mm diameter) to photoassociate atoms into molecules as shown in Fig. 3. The REMPI laser is a nano-second pulsed dye laser (Continuum ND6000) with a pulse energy of  $\sim 5$  mJ and a linewidth of  $\sim 0.5$   $\text{cm}^{-1}$  pumped by a Nd:YAG laser running at 532 nm with a 10 Hz repetition rate. The REMPI laser ionizes the atoms and molecules into  $\text{Rb}^+$  and  $\text{Rb}_2^+$ , respectively. A boxcar averager integrates the ion signal within the time of flight range of  $\text{Rb}_2^+$  ions. Our attempts to detect photoassociation by trap loss spectroscopy were unsuccessful; any decrease in MOT fluorescence was smaller than the fluorescence noise of the MOT.

#### 4 Photoassociation spectroscopy

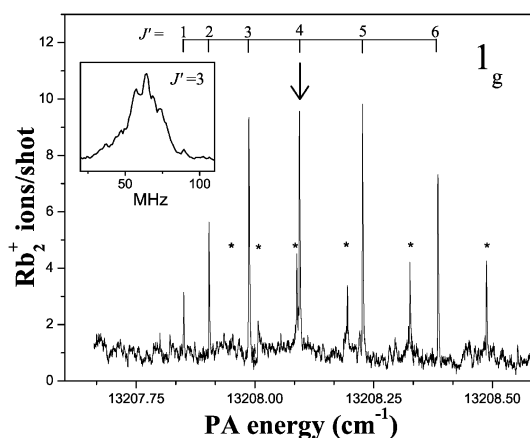
PA spectra were obtained by scanning the PA laser while monitoring the production of  $\text{Rb}_2^+$  formed by the REMPI laser. Typical photoassociation spectra are shown in Fig. 4–7. Each spectrum shows rotational lines, atomic “hyperfine ghost” lines, and in some cases molecular hyperfine lines.

If  $\Omega > 0$ , the electronic angular momentum can couple with the nuclear angular momentum, resulting in molecular hyperfine splittings. Hyperfine splittings are therefore expected for the  $2_g$  and  $1_g$  states, but not for the  $0_g^+$  and  $0_g^-$  states. We were able to resolve the molecular hyperfine splitting for the  $2_g$  states as shown in the inset of Fig. 4, but were unable to resolve the molecular hyperfine splitting for the  $1_g$  states (inset of Fig. 5) as the splittings are smaller than the observed linewidths.

The PA spectra show rotational lines up to a maximum of  $J' = 6$ , indicating the presence of s, p, d, and f partial waves in the collision of atoms.<sup>2</sup> This number of partial waves is consistent with the red-detuned PA spectra observed with the same setup. One notable difference is that for red-detuned photoassociation, lines with  $J' = 0, 1, 2$ , and 3 (arising from s and d partial waves) are stronger than lines with  $J' = 4, 5$ , and 6 (arising from d and f partial waves), while for blue-detuned photoassociation, lines with  $J' = 4, 5$ , and 6 are generally stronger than lines with  $J' = 0, 1, 2$ , and 3. The prevalence of high partial waves in blue-detuned PA could potentially be explained by some kind of heating process. We have ruled out an increase in steady-state temperature of the atoms caused by



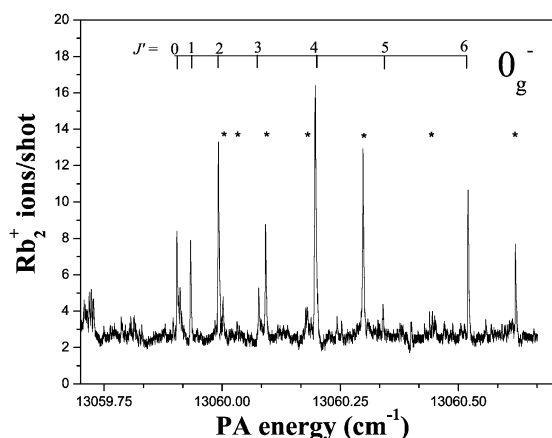
**Fig. 4** PA spectrum of the  $2_g v' = 2$  level. The inset shows a closeup of the  $J' = 6$  line showing molecular hyperfine structure. Rotational assignments are shown above the spectrum. Lines marked by an (\*) are atomic “hyperfine ghost” lines occurring  $0.1$   $\text{cm}^{-1}$  above each rotational line.



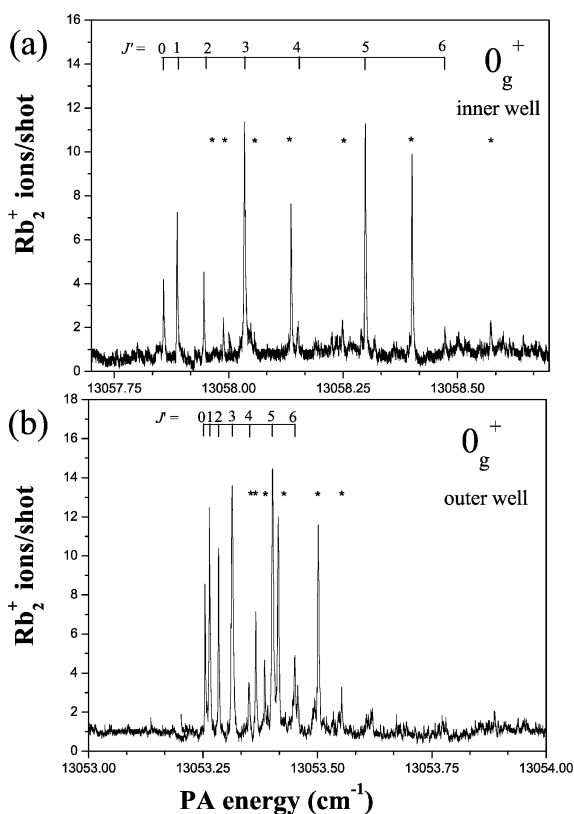
**Fig. 5** PA spectrum of the  $1_g v' = 8$  level. Rotational assignments are shown above the spectrum. The arrow ( $\downarrow$ ) indicates where the PA laser is fixed for the subsequent  $a^2\Sigma_u^+ v'' = 0$  REMPI spectrum. The inset shows a closeup of the  $J' = 3$  line where the molecular hyperfine lines are mostly unresolved. Lines marked by an (\*) are atomic “hyperfine ghost” lines occurring  $0.1$   $\text{cm}^{-1}$  above each rotational line.

the blue-detuned PA light, as the ballistic expansion with blue or red-detuned PA light is identical to the ballistic expansion without PA light. We suspect that the change in partial wave distribution between red and blue-detuned PA could be due to flux enhancement effects<sup>24,25</sup> created by the MOT light.

The energy of a rovibrational level is given to the first order by  $E_{v,J} = T_v + B_v[J(J+1) - \Omega^2]$ . Here  $T_v$  and  $B_v$  are the term energy and the rotational constant of a vibrational level, respectively.  $J$  is the rotational quantum number, which is always greater than or equal to  $\Omega$ . We extract the experimental rotational constant  $B_v^{\text{EXP}}$  by fitting a straight line to the energy of the rotational lines versus  $J(J+1) - \Omega^2$ , the results of which are tabulated in Table 1. This fitting process also allowed us to assign an  $\Omega$  quantum number to each spectrum. The experimental term energies  $T_v^{\text{EXP}}$  are simply the wavenumbers of the photoassociation laser plus the average thermal energy of collisions ( $\sim 10^{-4}$   $\text{cm}^{-1}$ ). The theoretical rotational constant  $B_v^{\text{THE}}$  and term energy  $T_v^{\text{THE}}$  are derived from the *ab initio* potential



**Fig. 6** PA spectra of the  $0_g^- v' = 3$  level. Rotational assignments are shown above the spectra. Lines marked by an (\*) are atomic “hyperfine ghost” lines occurring  $0.1 \text{ cm}^{-1}$  above each rotational line.



**Fig. 7** PA spectra of the  $0_g^+$  inner well  $v' = 3$  level (a) and the  $0_g^+$  outer well  $v' = 5$  level (b). Rotational assignments are shown above the spectra. Lines marked by an (\*) are atomic “hyperfine ghost” lines occurring  $0.1 \text{ cm}^{-1}$  above each rotational line.

energy curves using the LEVEL 8.0 program.<sup>21</sup> Assigning the vibrational quantum numbers to the spectra was greatly simplified by knowledge of the theoretical vibrational energy spacings. After assigning the vibrational numbers, we were able to determine the energy shift to the potential curves necessary make them match the experiment. These energy shifts were  $-61$ ,  $-27$ ,  $-61$ ,  $-51$ , and  $-100 \text{ cm}^{-1}$  for the  $0_g^+$ ,  $0_g^+$  outer well,  $0_g^-$ ,  $1_g$ , and  $2_g$  states, respectively. The unshifted potential energy curves can be found in ESI.†

**Table 1** Experimental and theoretical rotational constants ( $B_v$ ) and vibrational term energies for  $J' = 3$  ( $T_{v,J'=3}$ ) for levels of the  $1^3\Pi_g$  state in units of  $\text{cm}^{-1}$ . The theoretical term energies are shifted (see text) to match the experimental term energy of the lowest observed vibrational level. The area ( $A$ ) under PA spectral lines for  $J' = 3$  of the  $2_g$ ,  $1_g$ , and  $0_g^-$  states, and  $J' = 4$  of the  $0_g^-$  state in arbitrary units. This line area is an approximation of relative photoassociation rates

State	$v'$	$B_v^{\text{EXP}}$	$B_v^{\text{THE}}$	$T_{v,J'=3}^{\text{EXP}}$	$T_{v,J'=3}^{\text{THE}}$	$A$
$2_g$	0	—	0.01583	—	13029.293	—
	1	0.0152(9)	0.01568	13059.43(1)	13059.433	1.5
	2	0.01513(3)	0.01550	13089.04(1)	13088.595	1.0
	3	0.0156(3)	0.01530	13117.68(1)	13117.029	14
	4	0.0152(3)	0.01510	13145.44(1)	13144.457	1.1
	5	0.01470(1)	0.01488	13172.06(1)	13170.650	13
	6	0.0143(2)	0.01461	13197.47(1)	13195.609	1.2
	7	0.01382(8)	0.01431	13221.54(1)	13219.201	15
	8	—	0.01395	—	13241.166	—
	9	—	0.01349	—	13261.174	—
$1_g$	0	—	0.01278	—	13278.579	—
	0	0.0158(2)	0.01561	13008.610(1)	13008.610	8.6
	1	0.0154(2)	0.01543	13037.791(1)	13037.044	1.7
	2	0.01533(3)	0.01523	13065.957(1)	13064.479	14
	3	0.01494(6)	0.01500	13093.040(1)	13090.810	0.8
	4	0.0147(2)	0.01475	13119.053(1)	13115.910	7.2
	5	—	0.01446	—	13139.627	—
	6	0.01423(1)	0.01411	13166.936(1)	13161.752	14
	7	0.01370(2)	0.01366	13188.488(1)	13181.949	0.7
	8	0.01338(6)	0.01299	13207.987(1)	13199.580	4.8
$0_g^-$	0	0.0151(3)	0.015490	12980.840(1)	12980.840	1.9
	1	0.01507(3)	0.015288	13008.388(1)	13008.264	8.0
	2	—	0.015062	—	13034.674	—
	3	0.01465(5)	0.014816	13060.092(1)	13059.846	7.5
	4	—	0.014534	—	13083.558	—
	5	0.01408(2)	0.014187	13106.164(1)	13105.664	9.4
	6	0.01367(6)	0.013742	13126.527(1)	13125.874	3.6
$0_g^+$ inner well	7	—	0.013070	—	13143.518	—
	0	—	0.015489	—	12979.282	—
	1	0.01510(3)	0.015286	13006.693(1)	13006.693	5.3
	2	—	0.015058	—	13033.079	—
	3	0.01465(2)	0.014812	13058.035(1)	13058.223	10
	4	0.0141(1)	0.014530	13081.793(1)	13081.910	1.9
	5	0.01396(5)	0.014182	13104.167(1)	13103.983	7.0
$0_g^+$ outer well	6	0.01364(9)	0.013733	13124.408(1)	13124.144	2.2
	7	—	0.013049	—	13141.709	—
	0	0.00478(8)	0.004791	13005.612(1)	13005.612	0.8
	1	0.00463(8)	0.004828	13016.113(1)	13016.556	0.3
	2	0.00478(5)	0.004851	13026.170(1)	13026.942	4.0
	3	0.00463(7)	0.004859	13035.708(1)	13036.788	12
	4	0.00481(2)	0.004851	13044.764(1)	13046.068	5.1
	5	0.00504(9)	0.004818	13053.313(1)	13054.730	18
	6	—	0.004745	—	13062.674	—
	7	0.00472(2)	0.004561	13068.586(1)	13069.629	6.5

The areas under specific rovibrational lines of the  $1^3\Pi_g$  state are also listed in Table 1. This area is proportional to the product of the photoassociation rate and the ionization rate, the latter of which depends on the frequency of the REMPI laser. After varying the REMPI frequency for many of the PA scans in an effort to obtain the strongest  $\text{Rb}_2^+$  signal, we expect the reported line areas to roughly approximate the photoassociation rate. If one compares the calculated<sup>4</sup> photoassociation rate to the  $0_g^+$  outer well with these measured line areas, one can see similarities; namely, an increase in PA rate with vibrational levels followed by strong oscillations.

The lifetimes of levels of the  $1^3\Pi_g$  state can be reduced by tunneling through the potential barrier. This tunneling corresponds to a molecule dissociating into two free atoms, and is more likely to happen for higher vibrational levels



**Table 2** Energy splitting between ( $v' = 1, J' = 3$ ) levels for various states. The theoretical splitting is derived from the potential curves given in the ESI.† The experimental splitting is derived from Table 1

Splitting	Splitting type	Theory/ cm <sup>-1</sup>	Experiment/ cm <sup>-1</sup>
$2_g-1_g$	Spin-orbit	70.1	21.64(1)
$1_g-0_g^-$	Spin-orbit	19.2	29.403(1)
$0_g^+$ inner well- $0_g^+$ outer well	Well position	26.7	-9.420(1)
$0_g^-0_g^+$ inner well	Reflection symmetry	-0.5	1.695(1)

where the barrier is less high and narrower. The tunneling lifetime has been calculated for the analogous state in KRb<sup>26</sup> (the  $2^3\Pi$  state) and varies between quasi-infinite lifetimes for the  $v' = 0$  level and  $4 \times 10^{-12}$  s for the uppermost vibrational level. For Rb<sub>2</sub>, the calculated lifetime for the uppermost level of the  $0_g^+$  outer well<sup>3</sup> is 0.054 ns. This lifetime corresponds to a linewidth of 2950 MHz. So far we have not been able to observe strong broadening of the higher vibrational levels. In particular, we measure a total linewidth for the  $v' = 7$  level of the  $0_g^+$  outer well of less than 50 MHz, and for the  $v' = 8$  level of the  $1_g$  state, less than 25 MHz.

The quality of the present theoretical model for molecular spin-orbit can be assessed by looking at the energy shift of potential curves reported above, and the energy splitting between potential curves listed in Table 2. In the internuclear distance range of the inner wells, the potential curves resulting from the diagonalization of  $H_{so}^{diab}$  are very similar to the  $1^3\Pi_g$  adiabatic one (*i.e.* the diagonal element of  $H^{adia}$ ), which thus appears to be split into four different spin-orbit components. First of all, it is well known that this kind of quantum chemistry calculation usually predicts potential well depths like the one of the  $1^3\Pi_g$  curve with an accuracy of about 100 cm<sup>-1</sup>. The shifts reported above are thus consistent with this accuracy. The shifts are not the same for all curves, as they involve different Hund's case (*a*) curves with various individual accuracies: the  $0_g^+$ ,  $0_g^-$ , and  $1_g$  curves result from the coupling between  $^3\Pi_g$  and  $^1\Sigma_g^+$ , between  $^3\Pi_g$  and  $^3\Sigma_g^+$ , between  $^3\Pi_g$ ,  $^1\Pi_g$  and  $^3\Sigma_g^+$ , respectively, while the  $2_g$  curve involves only  $^3\Pi_g$ . Nevertheless, it is encouraging that the inner wells of all the states must be shifted by about the same amount to match the position of the experimental levels as described in Table 1. Due to the form of  $H_{so,\ddagger}$  the potential well of the  $1_g$  curve is almost unshifted compared to the one of the original  $1^3\Pi_g$  curve, as the shift of  $-51$  cm<sup>-1</sup> (the smallest among inner wells) illustrates. The shift is different for the inner and outer wells of the  $0_g^+$  curve, which is expected as the spin-orbit model is more accurate for large internuclear distances. The spin-orbit splitting between  $1_g$  and  $2_g$  curves (*i.e.* the spin-orbit coupling diagonal matrix element in  $H_{so}^{diab}$  for the  $2_g$  symmetry) is overestimated by about 49 cm<sup>-1</sup>. In contrast, that for the  $0_g^+$  and  $0_g^-$  symmetries is underestimated by 10 cm<sup>-1</sup>. Finally, the tiny splitting between the  $0_g^+$  and  $0_g^-$  curves can only be predicted, at best, to the right order of magnitude. This is not surprising, as that energy splitting is much smaller than other

energy splittings and beyond the accuracy of the present spin-orbit model.

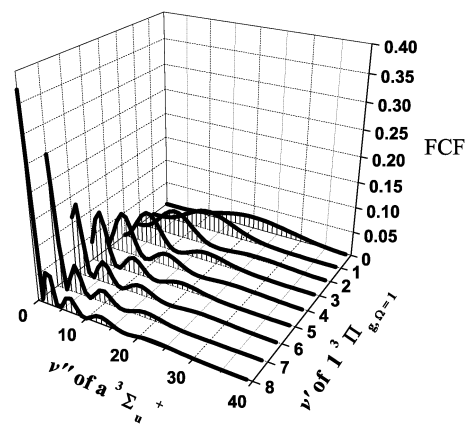
## 5 REMPI spectroscopy

Molecules in the  $1^3\Pi_g$  state spontaneously decay predominantly to the  $a^3\Sigma_u^+$  state. Spontaneous decay to the ground electronic state  $X^1\Sigma_g^+$  is forbidden due to the electric dipole (E1) selection rules for spin ( $\Delta S = 0$ ) and parity ( $u \rightarrow g$ ). The distribution of vibrational levels as a result of spontaneous decay can be approximated by the Franck-Condon factors connecting a single vibrational level of an upper state to a variety of vibrational levels of a lower state.

The Franck-Condon factors (FCFs) for spontaneous emission from  $1_g$  to  $a^3\Sigma_u^+$  are shown in Fig. 8; the largest FCF = 0.37 is between the  $v' = 8$  and  $v'' = 0$  levels. Therefore  $\sim 37\%$  of the molecules in the  $v' = 8$  level should decay to the  $v'' = 0$  level,  $\sim 31\%$  to all other vibrational levels  $v'' = 1$  to  $v'' = 39$ , and the remaining  $\sim 32\%$  to bound-free transitions that produce free atoms. The FCF's for emission from the  $2_g$ ,  $0_g^-$ , and  $0_g^+$  inner well to the  $a^3\Sigma_u^+$  state all have a similar distribution to the one plotted in Fig. 8. The highest FCF from  $2_g$  levels to  $v'' = 0$  is 30% starting from the  $v' = 9$  level. The highest FCF from the  $0_g^+$  inner well and  $0_g^-$  levels is 40% starting from the  $v' = 7$  level. The  $0_g^+$  outer well decays almost entirely between the  $v'' = 15$  and  $v'' = 30$  levels, regardless of the starting vibrational level  $v'$ .

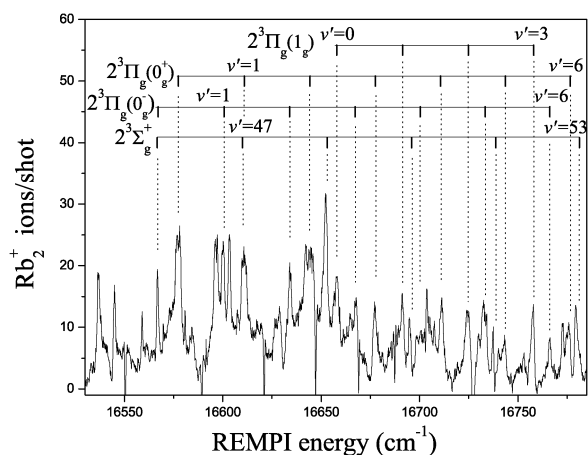
To produce a REMPI spectrum, we set the PA laser frequency on a chosen rovibrational level and scan the REMPI laser. With the PA laser set to the  $1_g$  ( $v' = 8, J' = 4$ ) level, we obtain a REMPI spectrum (Fig. 9) which shows that  $v'' = 0$  is present with a larger population than any other vibrational levels, as predicted by FCF's. Since the initial  $a^3\Sigma_u^+$  state population is mostly in a single vibrational level, the REMPI spectrum is simplified and displays mostly the structure of the intermediate states ( $2^3\Sigma_u^+$  and  $2^3\Pi_g$ ) rather than a combination of initial ( $a^3\Sigma_u^+$ ) and intermediate states.

The theoretical energies of REMPI transitions are calculated using the term energy of the  $a^3\Sigma_u^+$   $v'' = 0$  level and the term energies of the intermediate states. The term energy of the  $a^3\Sigma_u^+$   $v'' = 0$  level is calculated to be  $-234.73$  cm<sup>-1</sup> using



**Fig. 8** Franck-Condon factors for spontaneous emission between the  $1^3\Pi_g, \Omega=1$  and  $a^3\Sigma_u^+$  states. These calculations from LEVEL 8.0 are based on the  $1_g$  potential presented here and the  $a^3\Sigma_u^+$  potential.<sup>28</sup>

† The expressions of the  $H_{so}$  matrix for states correlated to an  $^2S + ^2P$  dissociation limit are displayed for instance in ref. 27, and those for the  $^2S + ^2D$  case in ref. 16.



**Fig. 9** REMPI spectrum with the PA laser frequency tuned to the ( $v' = 8, J' = 4$ ) level of the  $1_g$  state. Tick marks above the spectrum are theoretical transition energies between the  $a^3\Sigma_u^+$   $v'' = 0$  level and excited intermediate states  $2^3\Sigma_g^+$  and  $2^3\Pi_g(0_g^+, 0_g^-, 1_g)$ . These transitions account for most of the observed lines.

LEVEL 8.0 and the experimental  $a^3\Sigma_u^+$  potential.<sup>28</sup> The term energies of the intermediate states are calculated using LEVEL 8.0 and *ab initio* potentials<sup>8</sup> offset to match experimental data.<sup>16</sup>

## 6 Transition rates

The PA laser creates molecules in the  $1^3\Pi_g$  state, but these quickly decay to the  $a^3\Sigma_u^+$  state where their lifetimes are orders of magnitude larger. The radiative lifetime of the  $1^3\Pi_g$  state is  $\sim 20$  ns, while that of the  $a^3\Sigma_u^+$  state is estimated<sup>29</sup> to be on the order of 100 s. The lifetime of the  $a^3\Sigma_u^+$  state, however, is not limited here by radiative decay but instead by the amount of time the molecules reside in the REMPI beam before dropping ballistically ( $\tau_{\text{transit}} \approx 5$  ms). Since there are at any given moment orders of magnitude more molecules in the  $a^3\Sigma_u^+$  state than in the  $1^3\Pi_g$  state, the former state dominates the ionization process. The measured number of  $\text{Rb}_2^+$  ions is given by,

$$N_{\text{Rb}_2^+} = N_{a^3\Sigma_u^+} p_{\text{ionization}} e_d \quad (1)$$

where  $N_{\text{Rb}_2^+}$  is the number of  $\text{Rb}_2^+$  ions measured per REMPI pulse,  $N_{a^3\Sigma_u^+}$  is the steady state number of molecules in rovibrational levels of the  $a^3\Sigma_u^+$  state that are resonant with the REMPI laser,  $p_{\text{ionization}}$  is the photoionization probability per REMPI pulse, and  $e_d$  is the efficiency of the ion detector.

Several rovibrational levels of the  $a^3\Sigma_u^+$  state could be simultaneously resonant with different intermediate states whereby each would contribute to the total ion signal. However in the case of photoassociation to the  $v' = 8$  level of the  $1_g$  state, only the  $v'' = 0$  level contributes significantly to the ion signal.

Generally the first step of the REMPI process (bound-bound excitation) is fully saturated by the intense pulsed laser; however the second step of the REMPI process (bound-free photoionization) is not saturated and has a lower probability. We can calculate this ionization probability per pulse from,

$$p_{\text{ionization}} = 1 - e^{-Wt} = 1 - e^{-\frac{\sigma F}{I} t} = 1 - e^{-\sigma E \lambda / (hc \pi w^2)} \quad (2)$$

where the transition rate per second ( $W = \frac{\sigma F}{I}$ ) is given by the photoionization cross section ( $\sigma$ ) and the flux ( $F$ ) per unit time. The flux ( $F = E \lambda / (hc \pi w^2)$ ) is a measure of the total number of photons per unit area.  $E$ ,  $\lambda$ , and  $w$  are the pulse energy, wavelength and the Gaussian beam radius of the REMPI beam.  $h$  and  $c$  are Planck's constant and the speed of light. Although there are no known photoionization cross sections for the detection scheme we used, we can roughly estimate the cross section to be  $\sigma = 1_{-0.5}^{+5} \times 10^{-18} \text{ cm}^2$  based on other measurements.<sup>30,31</sup>

Taking for example the transition to the ( $v' = 8, J' = 4$ ) level of the  $1_g$  state, we observe  $N_{\text{Rb}_2^+} = 20$  molecules per REMPI pulse. With the following set of parameters ( $\sigma = 1_{-0.5}^{+5} \times 10^{-18} \text{ cm}^2$ ,  $E = 5 \text{ mJ}$ ,  $\lambda = 600 \text{ nm}$ ,  $w = 1.4 \text{ mm}$ ,  $N_{\text{Rb}_2^+} = 20$ , and assuming  $e_d = 1$ ) we obtain  $N_{a^3\Sigma_u^+} = 90_{-60}^{+80}$  molecules residing within the REMPI beam volume in the steady state.

Solving the rate equation for the number of  $a^3\Sigma_u^+$  state molecules, we obtain

$$N_{a^3\Sigma_u^+}(t) = \frac{R_{\text{PA}} \text{FCF} t}{1 + t/\tau} \quad (3)$$

where  $R_{\text{PA}}$  is the photoassociation rate per second,  $\tau$  is the transit time lifetime of  $a^3\Sigma_u^+$  molecules and FCF is the fraction of  $1^3\Pi_g$  molecules that decay to a particular vibrational level of the  $a^3\Sigma_u^+$  state. For the typical parameter values of  $\text{FCF} = 0.37$  and  $\tau_{\text{transit}} = 5 \text{ ms}$ , we obtain a photoassociation rate of  $\text{RPA} = 5_{-1.5}^{+4} \times 10^4$  molecules per second.

## 7 Conclusions

We have observed the formation of ultracold  $\text{Rb}_2$  molecules in the  $v'' = 0$  level of the  $a^3\Sigma_u^+$  state. The molecules are formed *via* blue-detuned photoassociation of the  $1^3\Pi_g$  state as proposed in ref. 4. We have performed spectroscopy of the  $1^3\Pi_g$  state and found good agreement with *ab initio* potentials. We have shown that the  $1_g$   $v' = 8$  level decays mainly to the  $a^3\Sigma_u^+$   $v'' = 0$  level. We expect equivalent schemes for photoassociation and ground state production to work for other alkali dimers. For instance,  $\text{K}_2^+$  and several heteronuclear alkali dimers<sup>32</sup> have blue detuned wells at short internuclear distance, in a situation analogous to the one for  $\text{Rb}_2$ .

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