## Spin noise spectroscopy of donor-bound electrons in ZnO

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We investigate the intrinsic spin dynamics of electrons bound to Al impurities in bulk ZnO by optical spin noise spectroscopy. Spin noise spectroscopy enables us to investigate the longitudinal and transverse spin relaxation time with respect to nuclear and external magnetic fields in a single spectrum. On one hand, the spin dynamic is dominated by the intrinsic hyperfine interaction with the nuclear spins of the naturally occurring <sup>67</sup>Zn isotope. We measure a typical spin dephasing time of 23 ns, in agreement with the expected theoretical values. On the other hand, we measure a third, very high spin dephasing rate which is attributed to a high defect density of the investigated ZnO material. Measurements of the spin dynamics under the influence of transverse as well as longitudinal external magnetic fields unambiguously reveal the intriguing connections of the electron spin with its nuclear and structural environment.

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Among the oxide-based II-VI semiconductors, ZnO has been devoted a continuously high attention in what concerns its optoelectronic properties<sup>1</sup> and possible application in semiconductor spintronics.<sup>2–4</sup> Especially the long electron spin coherence times at room temperatures which result from the rather weak influence of the spin-orbit splitting onto the conduction band states<sup>5,6</sup> make ZnO and ZnO nanostructures<sup>7</sup> a promising material in semiconductor spintronics and spinbased quantum optronics.<sup>8</sup> The semiconductor material ZnO is easily available with a high abundance and nowadays comes with a vast selection of growth and structuring methods.<sup>9</sup> Furthermore, ZnO bears a plethora of interesting spin physics due to its intriguing exciton dynamics<sup>10</sup> and scalability of hyperfine interaction between lattice nuclei and, e.g., electrons confined in colloidal quantum dots.<sup>11</sup> Besides the activities on single quantum dots in the context of quantum information processing,<sup>12</sup> the system of donor (acceptor) bound carriers in bulk semiconductors bears the potential of an extremely homogenous spin system which might compete with cold atomic gases in the near future, which concerns applications in quantum information processing.<sup>13,14</sup> In this work we investigate the intrinsic spin dynamics of donor-bound electrons in the wide-band-gap material ZnO by the emerging new technique of optical spin noise spectroscopy (SNS) in semiconductors via below-band-gap Faraday rotation. Spin noise spectroscopy measures the omnipresent fluctuations of the spin degree of freedom nearly perturbation free<sup>15-21</sup> and has developed into a powerful tool for the investigation of the intrinsic spin dynamics in semiconductors,<sup>22</sup> since it generally avoids optical excitation.<sup>23–25</sup> In the measurements presented here, SNS reveals the transverse and longitudinal spin relaxation of donor-bound electrons due to hyperfine interaction where only a low fraction of the host nuclei carry a nuclear spin. Both transverse and longitudinal times are acquired in a single spin noise spectrum by SNS, which allows the straightforward extraction of the influence of nuclear and external magnetic fields. Furthermore, we observe an additional, very short spin dephasing time which we attribute to the increased interaction with defects located inside the effective donor volume.

The present sample is a thin film of predominantly bulk, (0001)-grown ZnO with a nominal thickness of 450 nm deposited on a sapphire substrate by molecular beam epitaxy growth. The structure is not intentionally doped. However, an inclusion of Al-donor impurities is unambiguously identified by photoluminescence measurements as described below. The origin of Al inclusion is manifold. Besides Al being a residual contamination of the group-II constituent Zn, which gives rise to small amounts of Al in nearly every ZnO material,<sup>26</sup> a higher Al concentration as present in our investigated specimen results from the strong diffusion of Al from the Ål<sub>2</sub>O<sub>3</sub> substrate into the ZnO layer.<sup>27</sup> Further investigations of the thin-film sample by scanning electron microscopy reveal a nanoporous structure with a granularity varying between 10 and 20 nm at the surface. Henceforth, the investigated material most likely exhibits a high defect density induced by surface states, which is confirmed by a short photoluminescence lifetime at low temperatures which drops even further at elevated temperatures. Figure 1(a) depicts the time-resolved photoluminescence spectrum of the sample recorded with a synchroscan streak camera system under above-band-gap excitation with a frequency-doubled, picosecond Ti:sapphire laser oscillator.<sup>28</sup> The donor-bound exciton transition  $D^0X$ and its LO phonon replicas are clearly visible. The inset depicts the time transient of the  $D^0X$  transition decaying monoexponentially with a lifetime of  $\tau_l = 60$  ps measured at T = 4 K. The donor-bound exciton transition is the dominant optical transition. The spin dynamics of the donor-bound electrons is explored in the spin noise measurements presented later. For a better characterization of the donor-bound exciton transition, we performed cw photoluminescence (PL) and transmission measurements which are shown in Fig. 1(b). From the PL spectra we attribute the neutral  $D^0X$  (3.360 eV) and ionized  $D^+X$  (3.364) transition to Al impurities besides an unidentified background PL signal around the  $D^+X$ transition.<sup>29</sup> The shaded area in Fig. 1(b) indicates the spectral region where SNS measurements are performed in dependence of the probe photon energy detuning relative to the  $D^0X$ transition. These measurements are described further below.

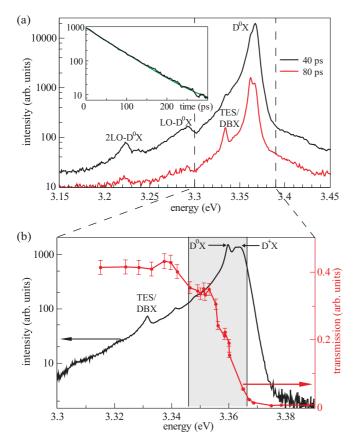


FIG. 1. (Color online) (a) Photoluminescence spectra recorded at 40 and 80 ps, respectively, after excitation with a picosecond laser pulse with a photon energy of 3.54 eV and a sample temperature of T = 4 K. The inset shows the PL decay transient of the donorbound  $D^0X$  exciton. (b) cw-PL (black line) recorded with a higher resolution. The labels  $D^0X$  and  $D^+X$  mark the spectral positions of the neutral and ionized donor-bound exciton transition, respectively. The red dots are transmission measurements performed with a spectrally narrow laser.

Figure 2 depicts the experimental setup for the measurements of the spin dynamics in transmission by spin noise spectroscopy. The light source is a frequency-doubled, cw-Ti:sapphire ring laser with a spectral width of 0.3 neV. The linear polarized light is focused down to a spot size with a typical diameter of 3  $\mu$ m and an intensity of 132  $\mu$ W/ $\mu$ m<sup>2</sup> and transmitted through the sample. The sample is mounted in a helium cold finger cryostat and cooled to a temperature of 4 K. The transmitted probe beam acquires the stochastic spin dynamics of the donor-electron spin ensemble in the ZnO sample via below-band-gap Faraday rotation. The timedependent, fluctuating Faraday rotation angle is analyzed by a polarization bridge consisting of a polarizing beam splitter and a balanced photoreceiver. Finally, the time-domain Faraday rotation data is analyzed via fast Fourier transformation (FFT) spectral analysis in the radio frequency regime on a standard personal computer.

The spin noise signal is low compared to the strong background optical shot noise and hence a background noise spectrum is recorded at a transverse magnetic field of  $\mathbf{B}_{\perp} = 10 \text{ mT}$ , which is then subtracted from the lower field spectrum. At  $\mathbf{B}_{\perp} = 10 \text{ mT}$ , the spin noise signal is completely shifted

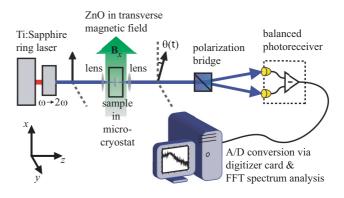


FIG. 2. (Color online) Experimental spin noise setup. The light source is a frequency-doubled cw-Ti:sapphire laser. The linear polarized probe light is focused through the sample which is mounted in a helium cold-finger cryostat. The rotation of the linear polarized light is measured by a polarization bridge and a balanced receiver. The electrically amplified difference signal is digitized in the time domain and spectrally analyzed by a computer. The external magnetic field can be applied in transverse and longitudinal (not shown) direction.

out of the measurable spectrum and hence only optical shot and electrical noise is recorded. Furthermore, the obtained noise spectrum is divided by the optical shot noise spectrum<sup>30</sup> in order to eliminate the nonuniform amplification of the balanced detector. The result is a normalized noise spectrum with only positive values (see Fig. 3). A typical monoexponential, i.e., homogeneous decay of the spin orientation with a decay constant  $\tau_s$  results in a Lorentzian-shaped spin noise contribution in the noise spectra with a full width given by  $\gamma_h =$  $1/(\pi \tau_s)$ . Inhomogeneities in the sample broaden the spin noise signal due to, e.g., g-factor variations or hyperfine interaction<sup>31</sup> and lead to a frequency spectrum following a normal distribution with a standard deviation  $\sigma_s$ . The inhomogeneous spin dephasing rate  $\gamma_i$  is finally given by  $2\sigma_s = \gamma_i/\pi$ .<sup>32</sup>

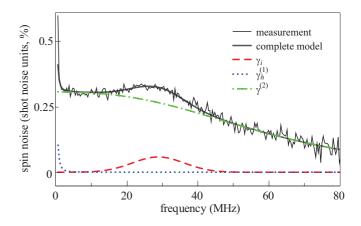


FIG. 3. (Color online) (a) Spin noise spectrum recorded with a *transverse* magnetic field of  $B_{\perp} = 1 \text{ mT}$  (black line). The background spectrum has been acquired at  $B_{\perp} = 10 \text{ mT}$  and the probe laser photon energy is 3.355 eV. The data is fitted by a model containing three spin noise contributions: an inhomogeneous contribution  $\gamma_i$  centered at the Larmor frequency  $\nu_L$  (red, dashed line), a homogenous contribution  $\gamma_h^{(1)}$  (blue, dotted line) centered around zero frequency, and a broad homogenous contribution  $\gamma_h^{(2)}$  (green, dashed dotted line) centered at the Larmor frequency  $\nu_L$ .

The spin noise spectra with applied transverse magnetic field  $\mathbf{B}_{\perp}$  reveal three distinct contributions which are depicted exemplarily in Fig. 3 for a single magnetic field. First, there is a very low homogeneous spin dephasing rate  $\gamma_h^{(1)}$  appearing as a Lorentzian-like peak centered at zero frequency. We attribute this contribution to the longitudinal spin relaxation rate of localized electrons with respect to the stochastic nuclear field orientation  $\mathbf{B}_N$  at the respective donor site. Second, there is an inhomogeneous spin noise contribution  $\gamma_i$  originating from the same localized electrons but which follows the applied transverse magnetic field with the respective Larmor frequency  $v_{\rm L} = g^* \mu_{\rm B} B / h$ . The magnitude of  $\gamma_i$  is given by the dispersion of  $\mathbf{B}_N$  within the ensemble of localized electrons. A third spin noise contribution with a very high homogeneous spin dephasing rate  $\gamma_h^{(2)}$  and centered as well at the Larmor frequency  $v_{\rm L}$  is attributed to donor-bound electrons interacting with one or more defects within the effective donor volume. This is discussed in more detail later. Figure 4(a) shows a series of spin noise spectra recorded with different transverse magnetic fields. The dependence of the Larmor frequency  $v_{\rm L}$ for the inhomogeneous contribution  $\gamma_i$  with magnetic field is shown in the inset of Fig. 4 and yields an effective Landé g-factor of  $g^* = 1.97(9)$ , which fits very well to the Landé gfactor of the Al-donor-bound electron as measured by electron paramagnetic resonance spectroscopy.<sup>33</sup> This assignment is consistent with the spectral identification of the  $D^0 X$  transition as elucidated in the previous section. Furthermore, the width of the inhomogeneously broadened spin noise spectrum, i.e.,  $\gamma_i$ , only shows a small linear dependence on **B**<sub> $\perp$ </sub> arising from g-factor inhomogeneities due to localization and  $\gamma_i$  is after all determined by the fluctuating nuclear field sampled by the localized electron wave function.<sup>31</sup> In ZnO only  $\frac{1}{2} \times 4.1\%$ of all lattice ions interact via hyperfine interaction with the donor electrons due the natural abundance of the <sup>67</sup>Zn isotope with a nuclear spin of  $I_N = 5/2$ . The electron wave function of an electron bound to an Al.donor has an effective Bohr radius of  $r_B = 1.93$  nm and thus experiences an interaction with  $\sim 5 \times 10^3$  nuclei. By taking the natural abundance of <sup>67</sup>Zn into account together with a Fermi-contact hyperfine interaction strength of 3.7  $\mu$ eV,<sup>11</sup> one obtains a standard deviation of the local magnetic field of  $\Delta B_N = 0.22 \text{ mT}$ , which corresponds to a theoretical limit for the inhomogeneous spin dephasing time of  $(\pi \gamma_i)^{-1} = 26.3$  ns. The inhomogeneous spin dephasing times extrapolated to zero magnetic field from the data presented in Fig. 4(a) yield  $T_2^* = 23(\pm 2.5)$  ns, matching very well to the theoretical expected times limited by the hyperfine interaction.

The longitudinal spin relaxation rate  $\gamma_h^{(1)}$  is defined with respect to the effective magnetic field axis, i.e.,  $\mathbf{B}_N + \mathbf{B}_{\perp}$ . The corresponding spin noise contribution appears as a narrow Lorentzian-like peak centered at zero frequency, as depicted in the presentation for the single noise contributions in Fig. 3. The spin noise power density at very low frequencies is usually superimposed by 1/f electrical noise, which makes a clear assignment of  $\gamma_h^{(1)}$  difficult. However, a longitudinal spin relaxation time  $(\pi \gamma_h^{(1)})^{-1} \gtrsim 200$  ns can be extracted even without taking into account the frequency range from dc to 0.5 MHz in the data evaluation. Furthermore, the observed spin noise power associated with  $\gamma_h^{(1)}$  decreases with increasing

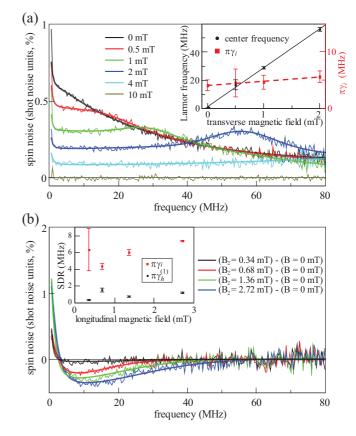


FIG. 4. (Color online) (a) Spin noise spectra recorded with different *transverse* magnetic fields. The background spectrum has been acquired at  $B_{\perp} = 10$  mT and the probe laser photon energy is 3.355 eV. The data is fitted by a model according to the description in the text. The inset depicts the change in the Larmor frequency (black solid line) and  $\gamma_i$  (red, dashed line) for the inhomogeneous spin noise contribution. (b) Spin noise difference spectra for different *longitudinal* magnetic fields. The spectra are shifted such that the average spin noise power density in the range of 50–80 MHz is zero in order to compensate for experimental drifts. The data is fitted according the model described in the text. The inset compares the homogeneous longitudinal ( $\gamma_h^{(1)}$ ) and inhomogeneous transverse ( $\gamma_i$ ) spin relaxation rates in dependence of  $B_{\parallel}$ . The probe laser photon energy is 3.359 eV for these measurements.

*transverse* magnetic field since the average projection of  $\mathbf{B}_N + \mathbf{B}_{\perp}$  onto the direction of observation decreases.<sup>34</sup>

The situation changes for external magnetic fields applied in *longitudinal*, i.e., *z* direction. Here an increasing magnetic field quenches the influence of the stochastic nature of the hyperfine interaction.<sup>25</sup> Figure 4(b) shows spin noise spectra obtained by measuring the difference between spin noise recorded with an applied longitudinal  $\mathbf{B}_{\parallel}$  and zero magnetic field. Clearly visible is that spin noise power from the inhomogeneous transverse part is redistributed to the homogeneous longitudinal spin noise contribution with increasing  $\mathbf{B}_{\parallel}$ . The total spin noise power is constant in thermal equilibrium, i.e., the external magnetic field is small compared to  $k_{\rm B}T/\mu_{\rm B}$  and polarization effects are negligible. The data presented in Fig. 4(b) is fitted by a single Lorentzian and Gaussian function both centered at zero frequency. The inset of Fig. 4(b) shows the spin dephasing rates  $\pi \gamma_i$  and  $\pi \gamma_h^{(1)}$ . The longitudinal spin dephasing rate is

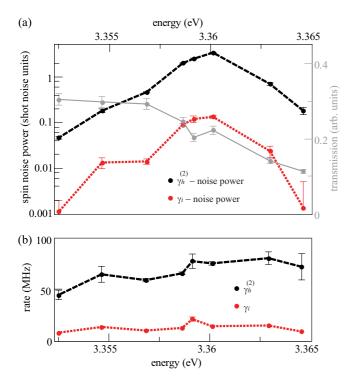


FIG. 5. (Color online) Dependency of (a) the total spin noise power and (b) spin dephasing rate on the detuning relative to the  $D^0X$  transition. The spectral position of the maximum spin noise power at 3.360 eV indicates that the major spin noise contribution originates from Al-donor-bound electrons.

slightly higher compared to the measurements with  $\mathbf{B}_{\perp}$  due to a smaller detuning from the optical resonance of the  $D^0 X$ in the corresponding measurements. In addition, we observe here that  $\pi \gamma_h^{(1)}$  does not explicitly decrease with  $\mathbf{B}_{\parallel}$ , which we attribute to a limitation of the minimal spin dephasing rate due to a remaining weak excitation of the donor-bound exciton transition, which in turn randomizes the spin orientation. A similar process has been observed in singly charged quantum dots,<sup>25</sup> where a residual excitation probability dictates the upper limit of the minimal detectable spin dephasing rate. The homogenous spin contribution with the very high spin dephasing rate  $\gamma_h^{(2)}$  cancels out in the difference measurements with longitudinal magnetic field due to the strongly dispersed spin noise power density.

In order to unveil the origin of the third, very fast homogeneous spin noise contribution  $\gamma_h^{(2)}$ , we perform spin noise measurements with a varying detuning with respect to the  $D^0X$  transition. Figure 5 compares (a) the spin noise

power and (b) the spin dephasing rate of the  $\gamma_h^{(2)}$  spin noise contribution with the inhomogeneous  $\gamma_i$  contribution. The spectral position of the maximum spin noise power at 3.360 eV indicates that the major spin noise contribution originates for both from Al-donor-bound electrons. However, the total spin noise power of the  $\gamma_h^{(2)}$  contribution is about one order of magnitude larger than the inhomogeneous contribution. The relative spin noise power scales with the contributing densities of spins such that we conclude that roughly 90% of all donor-bound electrons undergo a fast spin relaxation via defect-mediated spin scattering in conjunction with spin-orbit splitting. The exact mechanism is not clear at this point, but we assume an Elliot-Yafet-like spin dephasing mechanism where a high scattering rate leads to a higher probability of an electron spin flip.<sup>35,36</sup> Under the assumption that at least one defect within the donor volume already leads to a fast spin decay, we estimate a defect density  $n_d$  by relating the donor volume  $V_{Al}$  to the average defect volume  $V_d = n_d^{-1} = V_{Al}/0.9$ , which results in  $n_d = 3 \times 10^{19}$  cm<sup>-3</sup>. The high defect density is consistent with the nanocrystalline structure as measured by scanning electron microscopy. Furthermore, the spin dephasing rate  $\gamma_h^{(2)}$  is about one order of magnitude larger compared to  $\gamma_i$ . In fact, it is even higher than  $v_L$  for all measured magnetic fields (excluding the background acquisition). This in turn explains the non-Gaussian form of the spin noise contribution associated with  $\gamma_h^{(2)}$ , since the spin relaxation follows that of an overdamped oscillator, which can be approximated by an exponential, i.e., homogenous decay in the time domain.

In conclusion, we present all optical spin noise measurements on the wide-band-gap semiconductor material ZnO. All measured spin noise contributions are identified to originate from the Al-donor-bound electron in thermal equilibrium. The presented spin noise measurements unveil the rich physics of spin dynamics governed by the Overhauser nuclear field with the extracted inhomogeneous spin dephasing times being in accordance with the peculiar natural ZnO isotope composition. Most interestingly, we found additionally a strong defectmediated spin noise signal, giving rise to very short spin lifetimes, possibly originating from an Elliot-Yafet–like spinflip mechanism but which certainly deserves more extensive future investigations.

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<sup>5</sup>S. Ghosh, V. Sih, W. H. Lau, D. D. Awschalom, S.-Y. Bae, S. Wang, S. Vaidya, and G. Chapline, Appl. Phys. Lett. **86**, 232507 (2005).

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<sup>&</sup>lt;sup>1</sup>Ü. Özgür, J. Appl. Phys. 98, 041301 (2005).

<sup>&</sup>lt;sup>2</sup>I. Zutic, J. Fabian, and S. D. Sarma, Rev. Mod. Phys. 76, 323 (2004).

<sup>&</sup>lt;sup>3</sup>T. Dietl, H. Ohno, F. Matsukura, J. Cibert, and D. Ferrand, Science **287**, 1019 (2000).

<sup>&</sup>lt;sup>4</sup>S. Ghosh, D. W. Steuerman, B. Maertz, K. Ohtani, H. Xu, H. Ohno, and D. D. Awschalom, Appl. Phys. Lett. **92**, 162109 (2008).

<sup>&</sup>lt;sup>6</sup>N. Harmon, W. Putikka, and R. Joynt, Phys. Rev. B **79**, 115204 (2009).

<sup>&</sup>lt;sup>7</sup>N. Janßen, K. M. Whitaker, D. R. Gamelin, and R. Bratschitsch, Nano Lett. **8**, 1991 (2008).

- <sup>8</sup>W. K. Liu, K. M. Whitaker, A. L. Smith, K. R. Kittilstved, B. H. Robinson, and D. R. Gamelin, Phys. Rev. Lett. **98**, 186804 (2007).
- <sup>9</sup>A. Janotti and C. G. van de Walle, Rep. Prog. Phys. **72**, 126501 (2009).
- <sup>10</sup>D. Lagarde, A. Balocchi, P. Renucci, H. Carrère, F. Zhao, T. Amand, X. Marie, Z. X. Mei, X. L. Du, and Q. K. Xue, Phys. Rev. B 78, 033203 (2008).
- <sup>11</sup>K. M. Whitaker, S. T. Ochsenbein, A. L. Smith, D. C. Echodu, B. H. Robinson, and D. R. Gamelin, J. Phys. Chem. C **114**, 14467 (2010).
- <sup>12</sup>D. Loss and D. P. DiVincenzo, Phys. Rev. A 57, 120 (1998).
- <sup>13</sup>J. J. L. Morton, A. M. Tyryshkin, R. M. Brown, S. Shankar, B. W. Lovett, A. Ardavan, T. Sc henkel, E. E. Haller, J. W. Ager, and S. A. Lyon, Nature (London) **455**, 1085 (2008).
- <sup>14</sup>S. Simmons, R. M. Brown, H. Riemann, N. V. Abrosimov, P. Becker, H.-J. Pohl, M. L. W. Thewalt, K. M. Itoh, and J. J. L. Morton, Nature (London) **470**, 69 (2011).
- <sup>15</sup>F. Bloch, Phys. Rev. **70**, 460 (1946).
- <sup>16</sup>E. B. Aleksandrov and V. S. Zapasskii, Sov. Phys. JETP **54**, 64 (1981).
- <sup>17</sup>G. E. Katsoprinakis, A. T. Dellis, and I. K. Kominis, Phys. Rev. A **75**, 042502 (2007).
- <sup>18</sup>S. A. Crooker, D. G. Rickel, A. V. Balatsky, and D. L. Smith, Nature (London) **431**, 49 (2004).
- <sup>19</sup>H. Horn, G. M. Müller, E. M. Rasel, L. Santos, J. Hübner, and M. Oestreich, Phys. Rev. A 84, 043851 (2011).
- <sup>20</sup>S. A. Crooker, J. Brandt, C. Sandfort, A. Greilich, D. R. Yakovlev, D. Reuter, A. D. Wieck, and M. Bayer, Phys. Rev. Lett. **104**, 036601 (2010).
- <sup>21</sup>Q. Huang and D. S. Steel, Phys. Rev. B 83, 155204 (2011).

- <sup>22</sup>G. M. Müller, M. Oestreich, M. Römer, and J. Hübner, Physica E 43, 569 (2010).
- <sup>23</sup>G. M. Müller, M. Römer, D. Schuh, W. Wegscheider, J. Hübner, and M. Oestreich, Phys. Rev. Lett. **101**, 206601 (2008).
- <sup>24</sup>M. Römer, H. Bernien, G. Müller, D. Schuh, J. Hübner, and M. Oestreich, Phys. Rev. B 81, 075216 (2010).
- <sup>25</sup>R. Dahbashi, J. Hübner, F. Berski, J. Wiegand, X. Marie, K. Pierz, H. W. Schumacher, and M. Oestreich, Appl. Phys. Lett. **100**, 031906 (2012).
- <sup>26</sup>D. C. Look, in *Zinc Oxide Bulk, Thin Films and Nanostructures* (Elsevier, New York, 2006), pp. 21–42.
- <sup>27</sup>B. Pelcz, A. El-Shaer, A. Bakin, A.-C. Mofor, A. Waag, and J. Stoemenos, J. Appl. Phys. **100**, 103506 (2006).
- <sup>28</sup>J. Hübner and M. Oestreich, in *Spin Physics in Semiconductors*, edited by M. I. Dyakonov (Springer, Berlin, 2008), pp. 115–134.
- <sup>29</sup>C. F. Klingshirn, A. Waag, A. Hoffmann, and J. Geurts, *Zinc Oxide: From Fundamental Properties Towards Novel Applications* (Springer, New York, 2010).
- <sup>30</sup>The subtraction of the background noise power spectrum with the noise spectrum of the unilluminated detector yields the optical shot noise spectrum. Hereby the resulting spin noise power spectrum is expressed in units of optical shot noise power.
- <sup>31</sup>I. A. Merkulov, A. L. Efros, and M. Rosen, Phys. Rev. B **65**, 205309 (2002).
- <sup>32</sup>D. Pines and C. P. Slichter, Phys. Rev. **100**, 1014 (1955).
- <sup>33</sup>S. B. Orlinskii, J. Schmidt, P. G. Baranov, V. Lorrmann, I. Riedel, D. Rauh, and V. Dyakonov, Phys. Rev. B 77, 115334 (2008).
- <sup>34</sup>M. M. Glazov and E. L. Ivchenko, Phys. Rev. B 86, 115308 (2012).
  <sup>35</sup>R. J. Elliott, Phys. Rev. 96, 266 (1954).
- <sup>36</sup>Y. Yafet, R. W. Keyes, and E. N. Adams, J. Phys. Chem. Solids 1, 137 (1956).