

Dielectric properties of single wall carbon nanotubes-based gelatin phantoms

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In this work, we report the dielectric properties of Single wall Carbon Nanotubes (SWCNTs)-based phantom that is mainly composed of gelatin and water. The fabricated gelatin-based phantom with desired dielectric properties was fabricated and doped with different concentrations of SWCNTs (e.g., 0%, 0.05%, 0.10%, 0.15%, 0.2%, 0.4% and 0.6%). The dielectric constants (real ϵ' and imaginary ϵ'') were measured at different positions for each sample as a function of frequency (0.5–20 GHz) and concentrations of SWCNTs and their averages were found. The Cole–Cole plot (ϵ' versus ϵ'') was obtained for each concentration of SWCNTs and was used to obtain the static dielectric constant ϵ_s , the dielectric constant at the high limit of frequency ϵ_∞ and the average relaxation time τ . The measurements showed that the fabricated samples are in good homogeneity and the SWCNTs are dispersed well in the samples as an acceptable standard deviation is achieved. The study showed a linear increase in the static dielectric constant ϵ_s and invariance of the average relaxation time τ and the value of ϵ_∞ at room temperature for the investigated concentrations of SWCNTs.

Keywords: Single-wall carbon nanotubes; dielectric; relaxation time; Cole–Cole model.

1. Introduction

Carbon nanotube-based materials because of their high aspect ratio hold the promise of providing new revolutionary technological applications in many fields.^{1,2} The interaction of electromagnetic radiation (e.g., microwaves) with carbon nanotubes-based materials is one of the active research areas that has potential technological applications in industry and medical fields.^{3–6} Recently, there were many studies focused on the microwave effects in carbon nanotubes-based materials and its medical applications aiming to diagnose and cure diseases (e.g., cancer disease).^{7–11} In the medical research field area, to achieve the later aims, there is a high demand on the fabrication and characterization of phantoms that represent electrical properties of Human organ's tissues (e.g., breast tissues).

Usually, the desired phantoms that represent the dielectric properties of specific tissues in human body after being well characterized are doped with different types of carbon nanotubes or nanomaterials. For example, in recent publications (e.g., by Mashal *et al.*¹³), the microwaves' heating effect in such phantoms has been studied for different concentrations of single wall carbon nanotubes (SWCNTs) aiming for breast cancer diagnosis and cure.^{12–16} Most studies in this field focus on the fabrication of phantoms with real and imaginary dielectric constants (ϵ' , ϵ'') that are similar to a

desired Human tissue in the frequency range of interest.^{17–19} However, other dielectric parameters like static dielectric constant ϵ_s , the dielectric constant at the high limit frequency ϵ_∞ and the average relaxation time τ have drawn less attention.

Monitoring the evolution of the dielectric properties as carbon nanotubes or other dopants introduced to phantoms is crucial for studying and optimizing technological applications. Moreover, such monitoring can be used as an indication of dispersion of carbon nanotubes in phantoms.

In this work, the dielectric parameters of ϵ_s , ϵ_∞ and τ will be investigated as a function of SWCNTs concentration using the Cole–Cole model. The chosen phantom in this study is made mainly out of water and gelatin and no oil in its content (oil is usually used to produce phantoms that mimic tissues with low water percentage¹⁷). This study was conducted in the frequency range of 0.5 GHz to 20 GHz and at room temperature around 25°C.

In the rest of this paper, four sections will be presented as follows: in Sec. 2, the theoretical background of the dielectric properties of materials will be discussed, while in Sec. 3, a description of the sample preparation will be presented along with a description of the dielectric parameters measurement setup, Sec. 4 will go over the results and discuss them thoroughly, at the end, summary of the main conclusions will be presented.

2. Theory

There are many theoretical models that can be used to explain the dielectric properties of materials depending on the number of reorientational processes taking place in the material when an oscillating electric field is applied.²⁰ For materials with single reorientational process, the Debye relaxation model can be utilized to fully obtain the dielectric parameters of a material. The mathematical relation of Debye model which relates the complex dielectric constant ($\varepsilon^*(\omega) = \varepsilon' - i\varepsilon''$) with frequency of electric field can be rewritten as

$$\varepsilon^*(\omega) = \varepsilon_\infty + \frac{\varepsilon_s - \varepsilon_\infty}{1 + i\omega\tau}, \quad (1)$$

where ε_∞ is the permittivity measured at the high frequency limit of a polarizable entity when it is unable to respond to the electric field, ε_s is the limiting low frequency permittivity, ω is the angular frequency, i is $\sqrt{-1}$ and τ is the time characteristic of the response or relaxation time. For a material or a composite that has N characteristic responses, Debye formulation can be written as

$$\varepsilon^*(\omega) = \varepsilon_\infty + \sum_{m=1}^N \frac{\Delta\varepsilon_m}{1 + i\omega\tau_m}. \quad (2)$$

Here, $\Delta\varepsilon_m$ is the dielectric strength of the m th response and N is the order (number of terms) of Debye's relation. Plotting ε'' with ε' in the complex plane yields a semicircle that its center is on the horizontal axis at $(\frac{\varepsilon_s + \varepsilon_\infty}{2}, 0)$ with radius of $\frac{\varepsilon_s - \varepsilon_\infty}{2}$. However, for systems that have skewed semicircle, one can use the Havriliak–Negami model which is given as follows:

$$\varepsilon^*(\omega) = \varepsilon_\infty + \frac{(\varepsilon_s - \varepsilon_\infty)}{(1 + (i\omega\tau)^{1-\alpha})^\beta}. \quad (3)$$

A special case of the Havriliak–Negami formula is the Cole–Cole formula when $1 \geq \alpha > 0$ and $\beta = 1$ and the Cole–Davidson formula with $\alpha = 1$ and $1 \geq \beta > 0$. When using the Cole–Cole formula (assuming $1 - \alpha = n$), the real and imaginary dielectric constants can be written, respectively, as^{20,21}:

$$\varepsilon' = \varepsilon_\infty + (\varepsilon_s - \varepsilon_\infty) \frac{1 + (\omega\tau)^n \cos(\frac{n\pi}{2})}{1 + 2(\omega\tau)^n \cos(\frac{n\pi}{2}) + (\omega\tau)^{2n}}, \quad (4)$$

$$\varepsilon'' = (\varepsilon_s - \varepsilon_\infty) \frac{(\omega\tau)^n \sin(\frac{n\pi}{2})}{1 + 2(\omega\tau)^n \cos(\frac{n\pi}{2}) + (\omega\tau)^{2n}}. \quad (5)$$

Using Eqs. (4) and (5), the relation that relates ε'' with ε' is written as

$$\left(\varepsilon' - \frac{\varepsilon_s + \varepsilon_\infty}{2}\right)^2 + \left(\varepsilon'' + \frac{(\varepsilon_s - \varepsilon_\infty)}{2} \cot(n\pi/2)\right)^2 = \left(\frac{\varepsilon_s - \varepsilon_\infty}{2} \csc(n\pi/2)\right)^2. \quad (6)$$

The values of ε_s , ε_∞ and n can be extracted by fitting the experimental data with Eq. 6. The average relaxation time τ

can be obtained by finding the angular frequency ω at which the ε'' reaches its maximum value, so that $\tau = 1/\omega$. The angular frequency is equal to $2\pi f$, where f is the frequency in units of Hz.

3. Materials and Methods

In this part of the paper, the detailed procedure for the fabrication of the chosen phantom doped with SWCNTs and the experimental setup for measuring the dielectric properties are presented.

3.1. Fabrication of SWCNT-based Phantoms

In order to fabricate a phantom with desired dielectric properties, a simple procedure is considered to fabricate the phantom as in Refs. 17 and 22. In Ref. 22, many phantoms were made with the range of dielectric properties by varying the gelatin and oil percentage in the phantoms. However, in the current study to investigate the effect of SWCNTs addition only, it has been chosen to fix the concentration of oil in the samples to be 0% and to use water only. The following steps describe in details the fabrication procedure of the phantom and the addition of SWCNTs:

- (i) Starting with a 0.129 g of *p*-toluic acid measured using analytical balance and mixed with 6.43 mL (5.1645 g) of *n*-propanol, then the solution was heated with stirring in water bath (50°C) until all the *p*-toluic powder is dissolved and the solution becomes clear.
- (ii) Then, a 122.73 mL of deionized water was added to the prepared solution at room temperature, which will form a turbid solution.
- (iii) A 21.965 g of 200 bloom gelatin derived from bovine skin (Sigma Aldrich) was added to the turbid solution portion by portion with stirring at room temperature until the entire gelatin was wetted.
- (iv) The beaker with contents was wrapped with many layers of plastic film (an available commercial film is used) and held in a water bath of $\sim 90^\circ\text{C}$.
- (v) The mixture was heated at 90°C in a water bath until it became transparent and no air bubbles were suspended.
- (vi) The beaker was removed from the water bath and the mixture was stirred to produce uniformity, then any air bubbles on the surface are removed.
- (vii) Partially, the beaker immersed in a water bath of cool water (20–25°C) and stirred until it cools to 50°C , then removed from the water bath and the desired mass of SWCNTs is added (supplied by Cheap Tubes Co., with length of 0.5–2.0 μm , purity > 90 wt.% outer diameter 1–4 nm, MWCNTs content < 5 wt.%, ash < 1.5 wt.%).
- (viii) The mixture then stirred well until the carbon nanotube distributed uniformly within the solution and then it was sonicated in ultrasonic bath for 15 min at 50°C .

Table 1. The percentage of starting materials in the prepared phantom.

<i>p</i> -Toluic acid	<i>n</i> -Propanol	Deionized water	Gelatin	Formaldehyde
0.0861%	3.443%	81.643%	14.643%	0.1849%

(ix) The emulsion was stirred using a hot plate with stirrer for few min at 40°C and a 0.637 g of formaldehyde solution 37 wt.% in H₂O was added using a micropipette during the stirring step. Finally, continuing stirring the emulsion on the hot plat stirrer without heating until it cools to 25°C and then the formed material was poured in a small glass beaker for cooling and solidification. The percentage of the materials in the phantom is summarized in Table 1.

The flowchart in Fig. 1 summarizes the main steps to fabricate the phantom doped with the SWCNTs in this work. The phantoms were molded in cylindrical cups with a flat bottom with a diameter of 4.0 cm and a height of 3.0 cm. The fabricated phantoms with different concentrations of SWCNTs were left to cure for three days while covered with plastic film to prevent being exposed to air.

3.2. Dielectric properties measurements

In this study, the open-ended coaxial probe method was utilized to study the samples dielectric properties.^{23–25} The dielectric properties of the phantom were studied using a Network Analyzer (model E5071C) with a dielectric probe (open coaxial end probe — performance probe) both made by Keysight Company as demonstrated in Fig. 2. Before performing the measurement, the dielectric probe needs to be calibrated by measuring a short conducting plate and by measuring deionized water at room temperature. The calibration and measurement process were all performed at room temperature (~ 25°C).

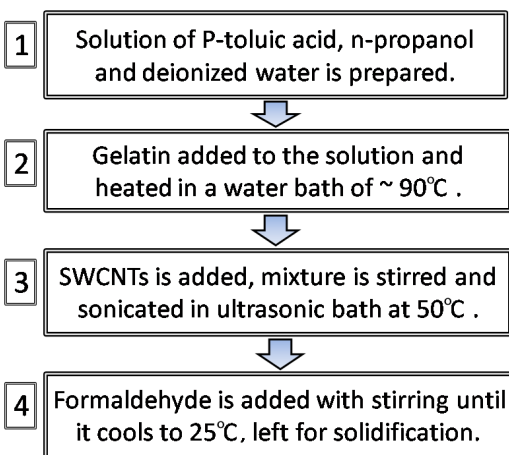


Fig. 1. The main steps of preparing the phantom that is doped with SWCNTs.

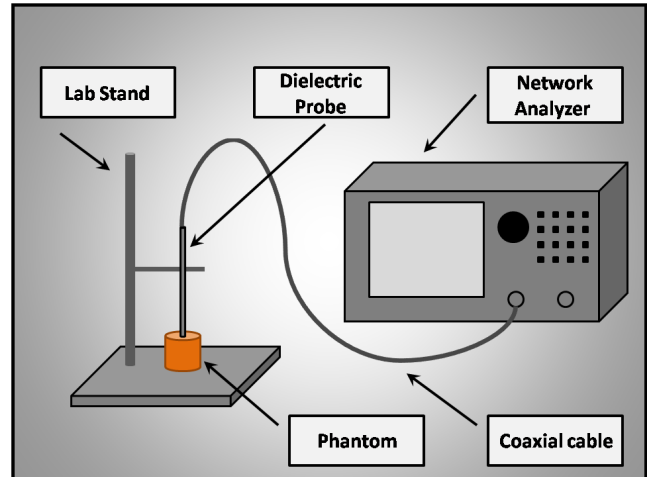


Fig. 2. The schematic diagram of the measurement setup used for studying the dielectric properties of the fabricated phantom.

In order to measure the dielectric properties that represent accurately the phantoms, the dielectric constants (real and imaginary) were measured at five different positions at the surface of the sample and their average is plotted with frequency.

4. Results and Discussion

The experimental setup for measuring the dielectric parameters presented in the previous section was used to measure the real and imaginary dielectric constants as a function of frequency as demonstrated in Fig. 3. It is clear in Fig. 3 that as the SWCNTs’ concentration is increased, the real and imaginary dielectric constants are increased too in the

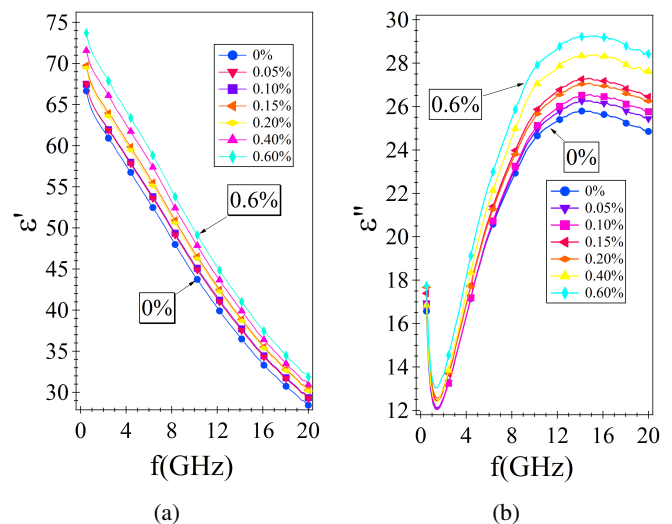


Fig. 3. (a) The real dielectric constant ϵ' and (b) the imaginary dielectric constant ϵ'' as a function of frequency for different concentrations of SWCNTs (each trace is the average of five measurements).

frequency range of 0.5 GHz to 20 GHz at room temperature. However, while the real dielectric constant is increased over the entire frequency range of 0.5 GHz to 20 GHz by the same amount approximately, the increase in the imaginary dielectric constant is larger in the high frequency range.

For the low frequency range (0.5 GHz to 1.5 GHz), the imaginary dielectric constant is attributed to the ionic conductivity generated from salt residues from gelatin powder during fabrication.²⁶ The relation ($\epsilon''_{dc} = \sigma_{dc}/\epsilon_0\omega$) provides the imaginary dielectric constant due to the contribution of ionic conductivity which is decreasing as the frequency is increased (σ_{dc} is the dc conductivity at the low frequency limit).

Since the measurement was performed at five different locations and their average was found, it is important to calculate the standard deviation (SD) to investigate the variance of ϵ' and ϵ'' from one location to another. The variation in the samples quality was investigated by monitoring the SD of the measurements for the l locations calculated for each concentration of SWCNTs using the following relation:

$$SD = \sqrt{\frac{\sum_{i=1}^l (\epsilon_i - \bar{\epsilon})^2}{l - 1}}, \quad (7)$$

where $\bar{\epsilon}$ is the average dielectric constant for the l locations at specific frequency. Figure 4 shows the calculated SD plotted for each SWCNTs concentration as a function of frequency for the real and imaginary dielectric constants. The values of the calculated SD are found to be around the typical accuracy of the used dielectric probe as provided by manufacturer $\Delta\epsilon' = \pm 0.05|\epsilon^*|$ and $\Delta\epsilon'' = \pm 0.05|\epsilon^*|$.²⁷ The reasonably small values of calculated SD are a strong indication of a good homogeneity of the samples and an indication of a good dispersion of SWCNTs in the phantom.²⁸

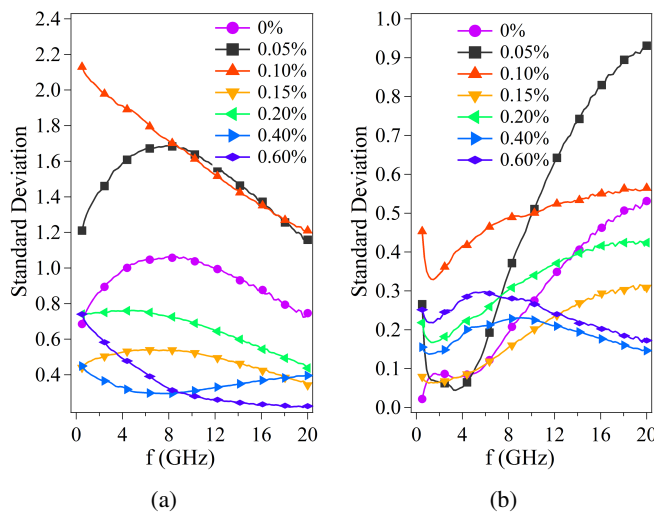


Fig. 4. The calculated SD for the measurements of (a) the real dielectric constant and (b) the imaginary dielectric constant as a function of frequency for all of the used SWCNTs concentrations.

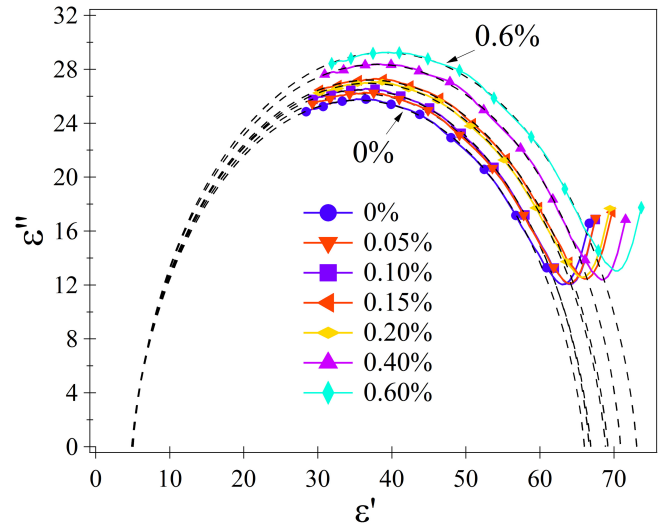


Fig. 5. The imaginary dielectric constant on the vertical axis as plotted with the real dielectric constant in the horizontal axis for different concentrations of SWCNTs that have been used in this study.

Moreover, in Fig. 4 one, can observe that as the applied frequency is increased; the obtained SD for the real dielectric constant is found to decrease for most concentrations and to increase for the imaginary dielectric constant.

The Cole–Cole plot is constructed for this study by plotting the imaginary dielectric constant on y-axis with real dielectric constant on x-axis as in Fig. 5. Using Eq. (6), the data in Fig. 5 can be fit and the dielectric parameters can be estimated for each SWCNTs concentration. In this study, it has been found out that to obtain good fit for the data, the value of α should be converging to 0.1 for all the concentrations of SWCNTs. The invariance of the value of the exponent α with SWCNTs concentration addition means that SWCNTs addition does not change the overall shape of the Cole–Cole plot. From the Cole–Cole plot fitting, the value of ϵ_∞ is directly estimated to be around 5 (close to ϵ_∞ of pure water at room temperature) and invariant with the addition of SWCNTs (see ϵ_∞ values in Table 2). The value of the static dielectric constant ϵ_s is found to be increasing linearly with a slope around 11.6 (per 1% of SWCNTs) and intercept on y-axis of 66.36 for zero concentration of SWCNTs.

The average relaxation time obtained using Eq. (6) is found to be around 10.4 ps and it is approximately invariant with the addition of SWCNTs as demonstrated in Table 2. One can explain this invariance of the dielectric parameters of ϵ_∞ and τ due to the large contribution of the phantom material relative to the dopant material which is around 0.6% at maximum. The invariance in the relaxation time can be explained by the fact that Eq. (6) provides the average relaxation time of many relaxation processes taking place in the samples. Such relaxation processes include the relaxation time of free water, bound water and the protein in the gelatin along with the SWCNTs contribution.^{29,30} Since the

Table 2. Dielectric parameters as obtained from Eq. (6) for different concentrations of SWCNTs.

	0%	0.5%	0.10%	0.15%	0.20%	0.40%	0.60%
ε_∞	4.9 ± 0.2	4.9 ± 0.2	4.9 ± 0.2	4.9 ± 0.2	4.9 ± 0.2	5.0 ± 0.2	4.8 ± 0.3
ε_s	66.0 ± 0.1	66.9 ± 0.1	66.7 ± 0.1	69.2 ± 0.1	68.9 ± 0.1	70.9 ± 0.1	73.0 ± 0.1
τ (ps)	10.30 ± 0.02	10.47 ± 0.01	10.36 ± 0.01	10.41 ± 0.01	10.42 ± 0.01	10.40 ± 0.01	10.40 ± 0.01
α	0.088 ± 0.001	0.114 ± 0.001	0.109 ± 0.002	0.114 ± 0.001	0.117 ± 0.001	0.104 ± 0.001	0.110 ± 0.001

concentration of SWCNTs is very small in the phantom, its contribution in the relaxation process is minimal. In order to be able to isolate the relaxation time due to the addition of SWCNTs, a wider frequency range is needed. With a wider frequency range, Eq. (2) can be used to find the dielectric parameters for the different relaxation process after the subtraction of ionic conductivity contribution from the imaginary dielectric constant.²⁶

5. Conclusions

In this study, the fabricated SWCNTs-based phantom samples are found to be in a good homogeneity and the SWCNTs are dispersed well in the samples as indicated by the obtained SD. Also, it has been confirmed that addition of SWCNTs can enhance the dielectric constants (real ε' and imaginary ε'') of phantoms as seen in Fig. 3. However, when the Cole–Cole model is used to obtain the dielectric parameters (e.g., ε_∞ , ε_s and τ), the parameters are found to be invariant with SWCNTs addition, except for the ε_s parameter which increases linearly with increasing SWCNTs concentration. The obtained average relaxation time is found to be approximately invariant with the addition of SWCNTs for the concentrations used in this study. The invariance of the average relaxation time could be attributed to the use of Cole–Cole fit that yields the average relaxation time of the (N) different reorientational processes (each has its τ_m and its dielectric strength $\Delta\varepsilon_m$).²⁰ Finding the exact values of τ_m and $\Delta\varepsilon_m$ for each process is found to be a difficult task due to the limitation in the used frequency range and due to the unavoidable contribution of the salt ions in the gelatin at low frequencies.

Finally, it is important to point out that the dielectric parameters of the fabricated phantom in this study can mimic the measured dielectric parameters of real human muscles and the gray matter (gray matter is a major component of the central nervous system).^{17,31} From the medical applications point of view, knowing the dielectric parameters of such phantom that is doped with SWCNTs may help in developing new methods of detection and treatment of cancer-infected tissues.¹³

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