

Precision Isotope Shift Measurements in Calcium Ions Using Quantum Logic Detection Schemes

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We demonstrate an efficient high-precision optical spectroscopy technique for single trapped ions with nonclosed transitions. In a double-shelving technique, the absorption of a single photon is first amplified to several phonons of a normal motional mode shared with a cotrapped cooling ion of a different species, before being further amplified to thousands of fluorescence photons emitted by the cooling ion using the standard electron shelving technique. We employ this extension of the photon recoil spectroscopy technique to perform the first high precision absolute frequency measurement of the ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transition in calcium, resulting in a transition frequency of $f = 346\,000\,234\,867(96)$ kHz. Furthermore, we determine the isotope shift of this transition and the ${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ transition for ${}^{42}\text{Ca}^+$, ${}^{44}\text{Ca}^+$, and ${}^{48}\text{Ca}^+$ ions relative to ${}^{40}\text{Ca}^+$ with an accuracy below 100 kHz. Improved field and mass shift constants of these transitions as well as changes in mean square nuclear charge radii are extracted from this high resolution data.

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Single or few laser-cooled ions trapped in Paul traps allow spectroscopy with high resolution and accuracy due to the near perfect realization of an unperturbed transition frequency as demonstrated in ion-based optical clocks [1]. For long-lived excited states the electron shelving technique provides near unity detection efficiency [2]. Advanced laser fluorescence techniques are well suited for closed or nearly closed broad, dipole-allowed transitions [3,4]. However, they provide insufficient signal to efficiently study nonclosed transitions where typically only one photon can be absorbed before the ion decays to a state which is not addressed by the spectroscopy laser. As a result, the fluorescence rate is low even when pump-repump techniques are employed [5,6], resulting in long averaging times for single ion experiments. Recently, new spectroscopy techniques with a high sensitivity to the absorption of single or few photons have been developed employing the signal from photon recoil [7,8] or decoherence of an electronic superposition state [9]. An evaluation of the dominant effects shifting the resonance from its unperturbed frequency provides accuracies below 100 kHz [4,8]. Up to now, these absolute frequency measurements have been demonstrated on nearly closed transitions.

Here, we demonstrate an extension of the photon recoil spectroscopy (PRS) technique [8] to perform an absolute frequency measurement of the nonclosed ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transition in ${}^{40}\text{Ca}^+$ with an accuracy of below 100 kHz. Using this extension together with the original PRS scheme, we performed isotope shift measurements of the

${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ and ${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ transitions for the most abundant even Ca^+ isotopes with an uncertainty below 100 kHz. These measurements improve the accuracy of the isotope shifts of the Ca^+ ions by up to 2 orders of magnitude compared to previous measurements [10,11].

From a multidimensional King plot analysis [12,13], seeded by the changes in mean square nuclear charge radii obtained from muonic atom spectroscopy and electron scattering, we derive improved values for the field and mass shift constants as well as the change in the mean square nuclear charge radius. The high accuracy of these measurements serves as a benchmark for *ab initio* atomic structure calculations and enables improved calibration for collinear laser spectroscopy [11,14], where typically uncertainties of a few MHz are achieved. These measurements are relevant for the investigation of nuclear properties of unstable calcium isotopes [15–17]. Calcium is of particular interest since its isotopes include two doubly magic nuclei at $A = 40$ and 48 . In the shell model, the additional eight neutrons form a complete $1f_{7/2}$ shell; however, there is little change in the mean-square proton radius (charge radius). Understanding these peculiar changes in the calcium charge radius is a challenge for nuclear theory [18].

We use the experimental setup for PRS with magnesium as the cooling ion species described in detail in [8,19,20]. In brief, we prepare two-ion crystals in a linear Paul trap consisting of ${}^{25}\text{Mg}^+$ and a selected Ca^+ isotope as the spectroscopy ion. Isotope-selective two-photon ionization is used to load the different Ca^+ isotopes: the ${}^1S_1 \rightarrow {}^1P_1$

transition of the neutral species of the target isotope is selectively excited using a narrow-linewidth laser [21], followed by ionization with a second laser. After loading, the isotopes are identified by the motional normal mode frequencies $\omega_{i,o}$ (i , in phase; o , out of phase) of the two-ion crystal in the axial trapping potential, given by [22,23],

$$\omega_{i,o}^2 = \omega_z^2 \left(1 + \mu \mp \sqrt{1 - \mu + \mu^2} \right), \quad (1)$$

where ω_z is the axial normal mode frequency of a single $^{25}\text{Mg}^+$ ion, $\mu = m_{\text{Mg}}/m_{\text{Ca}}$, and m_{Mg} and m_{Ca} are the masses of the two ions in the trap. Following the technique described in [22], the normal mode frequencies were measured and fits of the in-phase normal mode frequencies lead to 1.922(1), 1.889(1), 1.857(1), and 1.795(1) MHz for a two-ion crystal containing $^{40}\text{Ca}^+$, $^{42}\text{Ca}^+$, $^{44}\text{Ca}^+$, and $^{48}\text{Ca}^+$, respectively. The measured frequencies are in agreement with the frequencies calculated from (1) for the measured axial normal mode frequency of a single $^{25}\text{Mg}^+$ of 2.221(1) MHz.

Isotope shift measurements for the $^2S_{1/2} \rightarrow ^2P_{1/2}$ transition of the different Ca^+ isotopes were performed using the original PRS scheme [8]. The experimental sequence of the technique is displayed in Fig. 1(a). After Doppler cooling, we further cool the axial modes of the two-ion crystal to the motional ground state via sideband cooling on $^{25}\text{Mg}^+$ [20]. Starting from the motional ground state of one of the axial normal modes of the two-ion crystal, the spectroscopy laser with a wavelength of 397 nm is applied in 125 ns short pulses. The laser pulse repetition is matched to the motion of the two-ion crystal, thus enhancing the sensitivity through resonant driving and enabling the detection of around 10 absorbed photons with a signal-to-noise ratio of 1 [8]. A repump laser at 866 nm resonant with the $^2D_{3/2} \rightarrow ^2P_{1/2}$ transition is applied interleaved with the spectroscopy laser pulses to prevent populating the metastable $^2D_{3/2}$ state. The spectroscopy-repump cycles are repeated 70 times, obtaining the maximum motional excitation detectable without saturating the signal. The residual ground state population is measured using a red sideband stimulated Raman adiabatic passage (STIRAP)

pulse sequence coupling two ground state hyperfine levels in $^{25}\text{Mg}^+$ [24]. The sequence consists of one of the Raman beams being ramped up in intensity, while the other one is ramped down. This maps the motional excitation efficiently and independent of the motional state ($|n > 0\rangle$) into electronic excitation of the magnesium ion. The ground- and excited electronic states in $^{25}\text{Mg}^+$ are distinguished using the π detection technique [25]. It is based on two electron-shelving detection pulses with an interspersed state inversion using an rf π pulse. Keeping only anticorrelated detection events improves the detection fidelity.

We extend the original PRS scheme to measure the absolute frequency and the isotopic shifts of the open $^2D_{3/2} \rightarrow ^2P_{1/2}$ transition in Ca^+ as shown in Fig. 1(b). The sequence starts by initializing the Ca^+ ion in the $^2D_{3/2}$ state via optical pumping on the $^2S_{1/2} \rightarrow ^2P_{1/2}$ transition and subsequent sideband cooling on $^{25}\text{Mg}^+$. Absorption of a photon on the $^2D_{3/2} \rightarrow ^2P_{1/2}$ spectroscopy transition in Ca^+ results in a decay to the $^2S_{1/2}$ ground state with 94% probability [26], where the ion is lost from the normal spectroscopy cycle. Starting from the ground state of motion of one of the ion's normal modes, absorption of photons from a pulsed laser tuned to resonance with the $^2S_{1/2} \rightarrow ^2P_{1/2}$ transition in Ca^+ efficiently excites this motional mode analogously to the original PRS technique [8]. This corresponds to a first shelving step, since the excitation of phonons is conditional upon the absorption of a photon on the spectroscopy transition. Because of the nonvanishing probability of the ion to decay to the $^2D_{3/2}$ state the ion is effectively reinitialized in this state after 70 excitation pulses. Repeating the spectroscopy-motional excitation cycle three times further enhances the motion of the two-ion crystal to obtain the maximum motional excitation without reaching saturation. The motional excitation is mapped onto the $^{25}\text{Mg}^+$ ion and detected as before.

Commercially available external cavity diode lasers are used to excite the transitions of the different Ca^+ isotopes, where the laser coupling the $^2S_{1/2}$ and the $^2P_{1/2}$ state is frequency doubled to 397 nm. Both spectroscopy laser beams are aligned collinear with the axis of the linear Paul trap spanning a 45° angle with an external magnetic field required for efficient cooling and detection. The polarization is aligned perpendicular to the magnetic field to couple all magnetic substates of the involved transitions. The frequencies of both lasers are stabilized in the infrared to the frequency doubled output of a fiber-based optical frequency comb using an electronic feedback loop. A relative frequency stability of better than 10^{-12} is achieved with respect to the comb for averaging times of a second. The comb is stabilized to the 10 MHz reference signal obtained from a hydrogen maser, which is referenced to the SI second at the German National Metrology Institute.

The lasers are steered to the center frequencies of the spectroscopy transitions using acousto-optical modulators in double-pass configuration. We apply the two-point

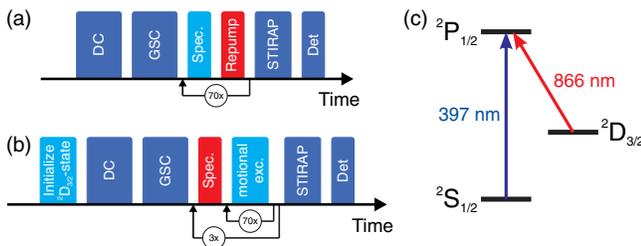


FIG. 1 (color online). Experimental sequence for the spectroscopy on (a) the $^2S_{1/2} \rightarrow ^2P_{1/2}$ transition and (b) the $^2D_{3/2} \rightarrow ^2P_{1/2}$ transition. A detailed description is given in the text. (c) Simplified level scheme of Ca^+ ions.

sampling technique [8], where the population difference at half maximum below and above the resonance line is measured and the difference is used to correct the center of the two probing frequencies for the next scan. The population difference in combination with the experimentally determined slope at these positions is used in post-evaluation to derive the center frequency of the atomic transition.

Following [8] we evaluated the dominant effects which could result in a shift of the observed transition frequency from its unperturbed value. External magnetic fields in combination with polarization asymmetries can cause an asymmetric line shape shifting the center frequency of the transition. Furthermore, the electrical field from the spectroscopy laser light may shift the frequency by means of the ac Stark shift, even though small intensities on the order of a few percent of the saturation intensity were employed for probing. Therefore, we measured the transition frequency for different magnetic fields and different spectroscopy laser intensities and extracted the corresponding shifts $\Delta f_{\text{Zeeman}} = 54 \pm 44$ kHz and $\Delta f_{\text{Stark}} = -70 \pm 83$ kHz for the experimentally used parameters. The given uncertainties correspond to the 68.3% prediction bound of the fit to the measured data and are limited by statistics. Because of the first shelving step in the newly developed technique, the dominant shift in the PRS technique, the so-called line shape shift arising from probe-frequency-dependent Doppler cooling and heating effects during motional excitation, is expected to be small. This was confirmed using density matrix simulations, where the shift was determined to be well below 1 kHz. The absolute frequency of the ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transition was derived as the weighted average of six frequency measurements and is given by $f = 346\,000\,234\,867(96)$ kHz, where 94 kHz of the uncertainty results from systematic and 21 kHz from statistical uncertainties.

We used the original and extended PRS technique to perform isotope shift measurements for the ${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ and ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transitions, respectively. The measurements of each isotope and the reference ${}^{40}\text{Ca}^+$ were performed interleaved. We first measured the ${}^{40}\text{Ca}^+$ transition frequency. Then, we loaded a new two-ion crystal containing the investigated isotope of Ca^+ and measured its transition frequency. After this, we repeated the measurement of the reference ion ${}^{40}\text{Ca}^+$ to ensure the absence of frequency drifts.

We investigated the statistical properties of all frequency measurements by plotting the overlapped Allan deviation $\sigma_y(\tau)$. No indication of drifts or other frequency fluctuations were observed for the performed measurements. As an example, the overlapped Allan deviation for the measurement of the ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transition of ${}^{40}\text{Ca}^+$ is shown in Fig. 2. After averaging, the measured frequencies were used to derive the isotope shift for each measurement. For the ${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ transition the measured isotope shifts

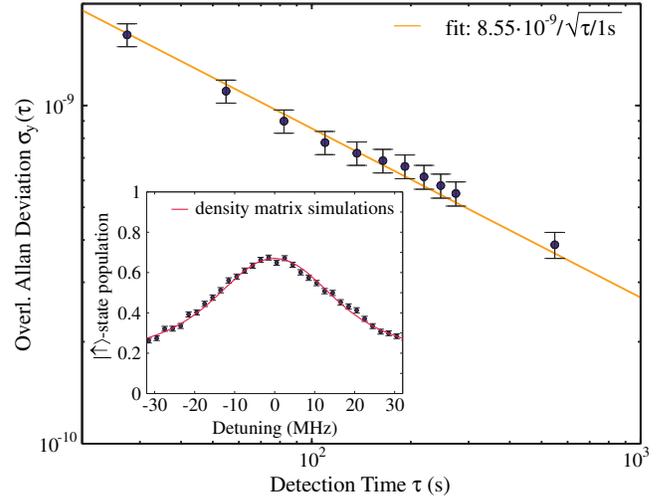


FIG. 2 (color online). Overlapped Allan deviation $\sigma_y(\tau)$ of the frequency measurement of the ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transition of ${}^{40}\text{Ca}^+$. The inset shows a resonance scan of the transition, where the red line corresponds to density matrix simulations adjusted in amplitude and offset to account for experimental imperfections.

were corrected by the change of the probe frequency-dependent line shape shift, resulting from the different mass of the isotope and the corresponding change of the normal mode frequency of the two-ion crystal. Using the simple model derived in [8], the calculated correction is smaller than 2 kHz per mass unit corresponding to a maximum correction of 10 kHz. All other systematic effects are common for the measurements performed on the same day and are therefore removed. The final values $\delta\nu^{A,40}$ with the corresponding accuracies are displayed in Table I.

Isotope shifts in atomic transition frequencies originate from two effects: a change in the size of the nucleus and thus its interaction with the electrons (field shift), and a change in the recoil of the nucleus (mass shift). The mass shift is more important for light elements, while for heavy elements the field shift dominates [27]. The difference in the transition frequency, $\delta\nu^{A,A'}$, between isotopes with mass m_A and $m_{A'}$ can be expressed as

$$\delta\nu^{A,A'} = k_{\text{MS}} \left(\frac{1}{m_A} - \frac{1}{m_{A'}} \right) + F \delta \langle r^2 \rangle^{A,A'}, \quad (2)$$

where k_{MS} is the mass shift constant, F is the field shift constant, and $\delta \langle r^2 \rangle$ is the change in the mean-square nuclear charge radius. The latter is a common parameter

TABLE I. Measured isotope shifts of the two transitions referenced to ${}^{40}\text{Ca}^+$.

A	$\delta\nu_{397}^{A,40}$ (MHz)	$\delta\nu_{866}^{A,40}$ (MHz)
42	425.706 (94)	-2349.974 (99)
44	849.534 (74)	-4498.883 (80)
48	1705.389 (60)	-8297.769 (81)

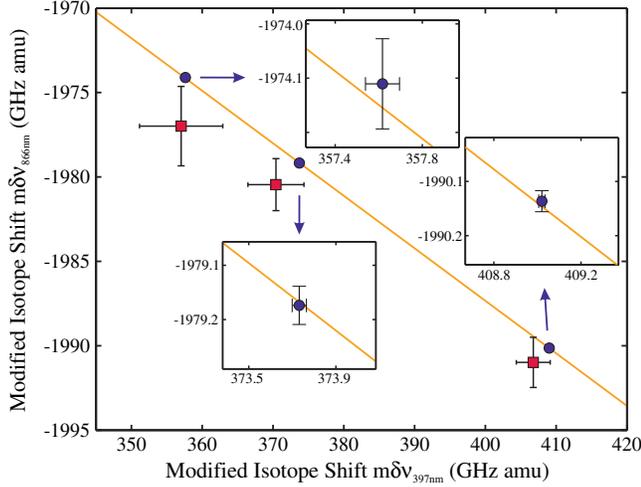


FIG. 3 (color online). Two-dimensional King plot showing the modified isotope shift of the 866 nm and 397 nm lines. Red squares, previous experimental data from [10] and [11]; blue circles, this Letter. The insets show the relevant ranges enlarged by a factor of approximately 30 to illustrate the quality of the fit.

when comparing two different transitions and can be eliminated in a King plot analysis [28,29] as shown in Fig. 3 for the two transitions considered here. Each axis shows the modified isotope shift $m\delta\nu^{A,A'} = \delta\nu^{A,A'} g^{A,A'}$, where $g^{A,A'} = (1/m_A - 1/m_{A'})^{-1}$, for one of the two transitions. A straight line fit to the three data points provides linear combinations of the field and mass shift constants for the two transitions. An important result from this fit is that there is no evidence for a deviation from a straight line, confirming that (2) is a good parametrization of the isotope shift even at the high experimental accuracy of the measurements presented here.

A comparison of the high resolution results with previous experimental data based on collinear laser spectroscopy [10,11] shows systematic deviations, which can be used to calibrate experimental parameters of this technique. Following Ref. [12] we performed a three-dimensional King plot analysis to extract the fitting parameters k_{MS} and F for the two transitions. Two dimensions are those shown in Fig. 3. In the third dimension we plot the modified change in mean-square nuclear charge radius $\delta\langle r^2 \rangle^{A,A'} g^{A,A'}$, using the previous values of $\delta\langle r^2 \rangle$ from [30], which are based on muonic atom spectroscopy and electron scattering. The three-dimensional King plot constrains the mass and field-shift constants, and under the assumption that (2) is correct (i.e., the three data points are connected by a straight line) can also be used to extract improved values of $\delta\langle r^2 \rangle$. To find the parameter estimates and their uncertainties an acceptance-rejection Monte Carlo method was used to generate samples consistent with the measured values and associated uncertainties [31]. The measurement distributions were assumed to be independent uncorrelated normals. The likelihoods of three randomly generated points, constrained to be collinear, were used as the acceptance criterion in the algorithm. The extracted parameters are shown in Table II.

The extracted field-shift and mass-shift constants pose a strong challenge for many-body atomic theory (fourth column of Table II), where the mass shift in particular has proven very difficult to calculate even in the “easy” case of single-valence-electron ions [32,33]. A comparison to the experimental field and mass shift constants given in [10,11] proves difficult since the derived uncertainties depend strongly on the analysis technique and input parameters for $\delta\langle r^2 \rangle$. Evaluating the field and mass shift constant from isotope shifts given in [10,11] using the

TABLE II. Parameters of three-dimensional King plot seeded with values of $\delta\langle r^2 \rangle^{A,40}$ taken from [30]. The units for the field F_i and mass k_i shift constants and the changes in mean square nuclear charge radii $\delta\langle r^2 \rangle^{j,40}$ are MHz fm^{-2} , GHz amu , and fm^2 , respectively. For comparison the second column for the previous data shows results for the analysis using isotope shift data taken from [10] and [11] analyzed with the methods used in this Letter.

Parameter	Previous	This work	Theory
F_{397}	$-283(6)^a$	$-281(34)$	$-281.8(7.0)$
k_{397}	$405.1(3.8)^a$	$406.4(2.8)$	$-285(3)^a$ -287^b 359^b 427^d
F_{866}	$79(4)^c$	$80(13)$	$87.7(2.2)$ 88^a 92^b
k_{866}	$-1989.8(4)^c$	$-1990.9(1.4)$	$-1990.05(13)$ -2207^b -2185^d
$\delta\langle r^2 \rangle^{42,40}$	$0.210(7)$	$0.210(7)$	$0.2160(49)$
$\delta\langle r^2 \rangle^{44,40}$	$0.290(9)$	$0.290(9)$	$0.2824(65)$
$\delta\langle r^2 \rangle^{48,40}$	$-0.005(6)$	$-0.005(6)$	$-0.0045(60)$

^aMårtensson-Pendrill *et al.* [10].

^bSafronova and Johnson [32].

^cNörtershäuser *et al.* [11].

^dThis work, based on the methods in [33].

analysis and input parameters employed here, indicates an order of magnitude improvement in these values based on the high resolution data presented here. Furthermore, the analysis leads to improved values of changes in mean-square nuclear charge radii which are in good agreement with the values derived from isotope shift measurements in neutral calcium [12].

In conclusion, we presented the first high precision absolute frequency measurement of the ${}^2D_{3/2} \rightarrow {}^2P_{1/2}$ transition in Ca^+ using an extension of photon recoil spectroscopy. We measured isotope shifts of this and the ${}^2S_{1/2} \rightarrow {}^2P_{1/2}$ transition of the most abundant stable, even isotopes in Ca^+ using this highly sensitive technique and improved the accuracy of the shifts by up to 2 orders of magnitude. From these measurements, improved values of the field and mass shift constants as well as changes in mean square nuclear charge radii are extracted. These results may serve to validate calculations and determine optimal models used in isotope shift calculations. Furthermore, the precise knowledge of the isotopic shifts can be used to improve the calibration of collinear laser spectroscopy experiments [15] and improve the analysis of quasar absorption spectra aimed at searches for variations of fundamental constants [34]. This Letter demonstrates that photon recoil spectroscopy is a versatile technique, suitable for a wide range of high precision spectroscopic applications.

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